

1 Revision 2

2 **Interpretation of the infrared spectra of the lizardite-nepouite series in the near and middle**
3 **infrared range**

4
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8

9 **Abstract**

10 A series of 1:1 silicate clays of the lizardite-nepouite series ($\text{Si}_2\text{Mg}_{3-x}\text{Ni}_x\text{O}_5(\text{OH}_4)$ with $x =$
11 0, 0.5, 1, 1.5, 2, 2.5, and 3) was synthesized at 220°C during 7 days from coprecipitated gels in
12 hydrothermal conditions. A clear relationship was evidenced between the d(06-33) and the Ni/Mg
13 ratio of the synthesized samples following a Vegard's law and suggested a rather random
14 distribution of octahedral cations. For the first time, infrared spectra of this series were given in
15 both near and mid infrared spectral regions (250 - 7500 cm^{-1}). Notably, the bands due to the OH
16 stretching vibrations and those of their first overtones in the lizardite-nepouite series were
17 attributed. The combination bands observed in the near infrared region for both end-members
18 could be attributed thanks to combinations of two or three mid infrared features. Some of the
19 observed combination bands are clearly linked to combination of different vibrational groups.

20 Infrared spectroscopy is simple to use and is a powerful tool to study the crystal-chemistry
21 of garnierites. More broadly, the improvement of band attributions especially in near infrared
22 contributes to develop the infrared analyses in field geology and remote sensing.

23 **Keywords:** lizardite, nepouite, infrared spectroscopy, near infrared, middle infrared, synthesis,
24 nickel, clay minerals, serpentine, phyllosilicates, garnierite

25

Introduction

26 Nickel ore deposits are found in lateritic or sulphide forms. The major part of produced Ni
27 comes from sulphide deposits (60 %) but Ni-laterite ores make up 60 to 70 % of the world's Ni
28 resources (Butt and Cluzel 2013). Ni concentration in laterites results from an intensive
29 weathering of ultramaphic rocks or their serpentized equivalents under tropical or rainforest
30 conditions like in New Caledonia (Wells et al. 2009) or Brazil (Mano et al. 2014). These deposits
31 are divided in two ore types, an oxidized one and a hydrous silicate type currently named
32 "Garnierite" (Faust 1966; Trescases 1975, 1979). The garnierite group is a general name for an
33 intimate mixture of hydrous Ni-Mg silicates that commonly includes two or more of the
34 following minerals: serpentine, talc, smectite and chlorite (Faust 1966; Brindley and Hang 1973;
35 Springer 1974; Brindley et al. 1979; Gleeson et al. 2004). Ni-bearing minerals in the serpentine
36 group are mainly lizardites and chrysotiles, whose Ni-analogs are nepouite and pecoraite.
37 Nepouite was first described by Glassere (1907) as the Ni-lizardite analog, and Maksimovich
38 (1973) showed the occurrence of the lizardite-nepouite series. The phyllosilicates belonging to
39 the lizardite-nepouite series are generally mixed with other minerals in garnierite. The study of
40 the crystal chemistry of these natural phyllosilicates is then uneasy. Moreover, as far as the
41 authors are aware, spectral data concerning this series are not available in literature, notably in
42 the near infrared (NIR) range ($4000 - 7000 \text{ cm}^{-1}$) although NIR field spectrometers could widely
43 be used by Ni-mining company for exploration. Field spectrometers are commonly used to
44 distinguish mineral compositional variations which may vary with the composition of altering
45 fluids, temperature and composition of host rocks in an alteration system. Mapping the
46 mineralogical variations at both geological scale with field/airborne/spaceborn infrared
47 spectrometer (Bowen et al. 2007; Di Tommaso and Rubinstein 2007; Chen et al. 2007;
48 Brandmeier et al. 2013) using NIR data and at the microscopic scale with infrared

49 microspectroscopy (IRMS) (Robin et al. 2013) using MIR data, contributes to improve the
50 understanding of the functioning of an alteration system and to determine the
51 mineralization/alteration relationships. In order to map mineralogical variations in lateritic Ni ore
52 deposit, spectral data in NIR range on the nepouite-lizardite series must be known. And
53 generally, even if spectral data exist for clay minerals, any band interpretations in NIR range are
54 made.

55 Therefore samples from the lizardite-nepouite series were synthesized to obtain pure
56 reference samples for a Fourier transform infrared (FTIR) study, in both NIR and mid infrared
57 (MIR) regions and band attributions were made.

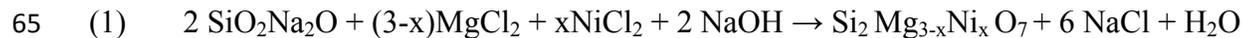
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Experimental

60 Clay synthesis

61 Samples of the lizardite-nepouite series were synthesized using a coprecipitated gel as
62 starting material as in Baron et al. (2016). Coprecipitated gels of $\text{Si}_2\text{Mg}_{3-x}\text{Ni}_x\text{O}_7$ theoretical
63 composition with $x = 0, 0.5, 1, 1.5, 2, 2.5,$ and 3 were obtained by mixing solutions of sodium
64 silicate, Mg and/or Ni chloride and sodium hydroxide (reaction 1).



66 After precipitation, the gel was collected by filtration and gently washed with deionized
67 water to remove sodium chloride and then dried at 60°C for 48 hours before being crushed. 0.5 g
68 of the powdered gel were placed into Teflon coated metallic bombs with 30 ml of deionized
69 water and heated at 220°C during one week under equilibrium vapor pressure. The solid was
70 separated from the solution by filtration and dried overnight at 60°C.

71 A synthetic Ni-Mg kerolite was also used in this study for comparison. The synthesis was
72 done using the same way than for lizardite-nepouite series from a coprecipitated gel with
73 $\text{Si}_4\text{Mg}_{1.5}\text{Ni}_{1.5}\text{O}_{11}$ theoretical composition obtained following the reaction (2):



75 **Analysis**

76 X-ray diffraction (XRD) powder patterns were performed with a Bruker D8 advance
77 diffractometer (CuK α radiation, 40 kV and 40 mA) over the range 2 - 65°2 θ , with 0.025°2 θ step
78 size and 0.6 seconds per step. The reflection (06-33) was recorded with a step of 0.025°2 θ and a
79 counting time of 4 seconds over the range 57 - 63°2 θ . The position of the (06-33) reflection was
80 determined by fitting XRD patterns with a pseudo-Voigt component in the Fityk software
81 (Wojdyr 2010).

82 A Magna-IR 760 Nicolet spectrometer was used for mid infrared spectra over the range
83 400 - 4000 cm^{-1} , with an EverGlo source, a KBr beam splitter, a DTGS-KBr detector and a
84 resolution of 4 cm^{-1} with co-additions of 100 scans. Over the range 200 - 500 cm^{-1} , a Thermo
85 Scientific Nicolet 6700 FT-IR spectrometer was used with an EverGlo source, a CsI beam
86 splitter, a DTGS-CsI detector and a resolution of 4 cm^{-1} with the co-additions of 100 scans. MIR
87 spectra were obtained in transmission through KBr pellets, prepared with 1 mg of sample and 150
88 mg of KBr salt. The mixture was pressed during 5 minutes at 8 kbar and dried overnight in an
89 oven at 110°C.

90 NIR spectra (3850 - 7500 cm^{-1}) were acquired with a Thermo Scientific Integrating
91 Sphere (diffuse reflectance) equipped with an internal InGaAs detector, set on a Thermo
92 Scientific Nicolet 6700 FT-IR spectrometer. A white light source was used, associated with a

93 CaF₂ beam splitter. The resolution was set at 4 cm⁻¹ with the co-additions of 100 scans. Powder
94 samples were analyzed directly on the integrating sphere without dilution.

95 The second derivative was carried out using the Savitzky–Golay filter (Savitzky and
96 Golay 1964) in the Omnic™ software with a set of 13 points and a polynomial order of 3. The
97 second derivative was used to determine the position of NIR and MIR bands, and was given in
98 inverted form in this study to facilitate the reading of spectra.

99 The deviation in band position possibly induced by the second derivative method was
100 estimated from a mathematical model. The model generated theoretical spectra by varying the
101 relative intensities of 2 pseudo-Voigt components, with a 4 cm⁻¹ resolution (as for experimental
102 spectra). The second derivative of these theoretical spectra was carried out as described above for
103 experimental spectra. The maximum deviation measured between the band positions introduced
104 in the model and the band positions measured from the second derivative was +/- 3 cm⁻¹.

105

106

Results and discussion

107 XRD data

108 XRD powder patterns of all samples exhibited an intense (001) reflection at 7.39 Å and a
109 (002) located at 3.67 Å for lizardite (x = 0) and at 3.64 Å for nepouite (x = 3), characterizing a
110 1:1 phyllosilicate structure. The (*hk*) reflections for lizardite (x = 0) and nepouite (x = 3) were
111 situated at 4.51 and 4.50 Å (020), 2.59 and 2.63 Å (200), 2.47 Å (201), and at 1.537 and 1.529 Å
112 (06-33), respectively (Fig. 1 and 2), revealing a trioctahedral structure. All (*hkl*) reflections were
113 in agreement with data reported in literature for natural lizardite and nepouite samples (Whittaker
114 and Zussman 1956; Mikheev 1957; Montoya and Baur 1963; Maksimovich 1973; Frondel and Ito
115 1975; Brindley and Brown 1980; Mellini 1982). XRD powder patterns revealed that no other
116 crystalline phases were present for all samples.

117 The d(06-33) continuously shifted from 1.537 Å for lizardite ($x = 0$) to 1.529 Å for
118 nepouite ($x = 3$) (Fig. 2). The d(06-33) value determined by fitting data with a single pseudo-
119 Voigt component, was plotted versus the Ni contents (x), and a clear correlation was evidenced
120 (Fig. 3) with the following regression line:

$$121 \quad d(06-33) (\text{Å}) = -0.0026 x + 1.5374 (1)$$

122 This relation followed an apparent Vegard's law suggesting a random distribution of
123 cations in the octahedral sheet of the synthesized samples. The progressive change of the d(06-
124 33) along the lizardite-nepouite series is due to the atomic radii difference between Ni and Mg
125 atoms in octahedral coordination (0.72 Å for Mg and 0.69 Å for Ni; Shannon 1976).

126

127 **MIR data**

128 **The OH-stretching zone.** The spectrum of the synthetic lizardite ($x = 0$) was similar to
129 the natural one (Serna et al. 1979; Fuchs et al. 1998; Balan et al. 2002), with a complex band at
130 3698 cm^{-1} enlarged to 3688 cm^{-1} (which will be discussed later), and a broad band at 3648 cm^{-1}
131 (Fig. 4). The former complex band at 3698 cm^{-1} corresponded to the in-phase stretching of the
132 inner-surface $\text{Mg}_3\text{-OH}$ groups and the latter at 3648 cm^{-1} to the two degenerate out-of-phase
133 stretching modes of the inner-surface $\text{Mg}_3\text{-OH}$ groups (Balan et al. 2002).

134 The increase of Ni contents in samples induced the progressive appearance of bands at
135 3686 cm^{-1} , 3668 cm^{-1} , and 3648 cm^{-1} . Finally, for nepouite ($x = 3$), only the band at 3648 cm^{-1}
136 was present with a broad band at around 3610 cm^{-1} (Fig. 4). By analogy with the spectrum of the
137 lizardite ($x = 0$) end-member, these two bands were assigned to the in-phase stretching of the
138 inner-surface $\text{Ni}_3\text{-OH}$ groups and to the two degenerate out-of-phase stretching modes of the
139 inner-surface $\text{Ni}_3\text{-OH}$ groups, respectively.

140 In trioctahedral phyllosilicates, each hydroxyl group is bonded to three octahedral cations
141 and the nature of these cations modifies the stretching vibration of hydroxyl groups. In the
142 lizardite-nepouite series, when Mg is partially replaced by Ni or conversely, four stretching OH
143 (ν OH) bands may be possibly distinguished due to the four possible cations combinations in the
144 three neighboring octahedral sites as it is well known for talc series: ν Mg₃-OH, ν Mg₂R²⁺-OH,
145 ν MgR²⁺₂-OH and ν R²⁺₃-OH where R²⁺ is the substituted cation (Wilkins and Ito 1967; Petit et al.
146 2004; Petit 2005, 2006; Madejová et al. 2011). Consequently, the two bands at 3686 and 3668
147 cm⁻¹ (Fig. 4) could be assigned to ν Mg₂Ni-OH and ν MgNi₂-OH, respectively.

148 **The 500-800 cm⁻¹ region.** The spectrum of lizardite ($x = 0$) revealed three bands at 634,
149 607 and 562 cm⁻¹ (Fig. 4). These bands, characteristic of pure Mg-lizardite, were assigned, after
150 IR spectra calculation, to longitudinal (LO) and transversal (TO) modes of in-plane bending of
151 OH groups (Balan et al. 2002; Prencipe et al. 2009). Very often, natural lizardite samples contain
152 some Fe²⁺ or Ni²⁺, and exhibit a broad band rather than these three distinguishable bands (Balan
153 et al. 2002). As a matter of fact, the three bands occurrence is a good criterion to easily determine
154 the Mg-purity of lizardite. For nepouite ($x = 3$), a broad and dissymmetric band at 674 cm⁻¹ with
155 a shoulder at 600 cm⁻¹ was observed. The intermediary samples ($0.5 < x < 2.5$) of the solid-
156 solution exhibited a broad and complex multicomponent band (Fig. 4).

157 **The lattice bands.** Two main bands located at 984 and near 1080 cm⁻¹ (Fig. 4) were
158 observed for all samples (Fig. 4). These bands were attributed to the two degenerate equatorial
159 stretching of Si-O bonds and the symmetric stretch of apical Si-O bonds, respectively (Balan et
160 al. 2002). The former band remained at 984 cm⁻¹ whatever the Ni content (x), whereas the latter
161 band was at 1084 cm⁻¹ for lizardite ($x = 0$) and moves progressively to 1075 cm⁻¹ for nepouite (x
162 = 3). A small shoulder at 1024 cm⁻¹ was observed for Mg-rich samples and disappeared with the
163 increase of Ni content (x) (Fig. 4). This shoulder was attributed to a LO mode (Prencipe et al.

164 2009) and could not be attributed to small amount of chrysotile because it would be associated to
165 an intense band at 960 cm^{-1} (Farmer 1974; Anbalagan et al. 2010; Madejová et al. 2011).

166 The lizardite ($x = 0$) spectrum exhibited bands at 454, 436, 400, 383, and 303 cm^{-1} while
167 the nepouite ($x = 3$) spectrum exhibited bands at 455, 426, 377, 361, and 318 cm^{-1} (Fig. 4). The
168 lizardite ($x = 0$) experimental spectrum was in agreement with the calculated spectra (Balan et al.
169 2002; Prencipe et al. 2009). For the intermediary samples ($0.5 < x < 2.5$), the bands moved
170 progressively and were at intermediate position between those of the lizardite ($x = 0$) and
171 nepouite ($x = 3$) end-members.

172

173 **NIR data**

174 The occurrence of a broad and intensive OH-water combination band around 5205 cm^{-1}
175 (Hunt and Salisbury 1970) in all spectra (Supplementary file a), revealed the relatively high water
176 content in samples, as it is very common for synthetic phyllosilicates. The high hydration state of
177 synthetic phyllosilicates is generally due to their small particle size (Dumas et al. 2013).

178 **The first OH overtone region.** By analogy with the MIR νOH region, the bands at 7226,
179 7198, 7164 and 7124 cm^{-1} (Fig. 5) were assigned to $2\nu\text{Mg}_3\text{-OH}$, $2\nu\text{Mg}_2\text{Ni-OH}$, $2\nu\text{MgNi}_2\text{-OH}$ and
180 $2\nu\text{Ni}_3\text{-OH}$. As for the MIR region, the presence of four $2\nu\text{OH}$ bands with relative intensities
181 varying continuously all along the solid-solution series argued for a rather random distribution of
182 Ni and Mg atoms in the octahedral sheet of the samples. The lack of a band at 7236 cm^{-1}
183 confirmed the absence of chrysotile (Madejová et al. 2011).

184 The anharmonicity constant between the νOH and $2\nu\text{OH}$ wavenumbers of the lizardite-
185 nepouite series is $X = -85.6\text{ cm}^{-1}$, that is the same value measured by Petit et al. (2004) for talcs
186 and others phyllosilicates (Fig. 6). This relation gives confidence for the above NIR assignments.

187 The NIR spectrum of lizardite ($x = 0$), exhibited a shoulder at 7203 cm^{-1} which could not
188 be attributed to the $2\nu\text{Mg}_2\text{NiOH}$ overtone (Fig. 5). This band may be attributed to the overtone of
189 the shoulder at 3688 cm^{-1} observed in the MIR spectrum according to the anharmonicity constant
190 value of -86.5 cm^{-1} . These bands may be due to vibrations of structural $\text{Mg}_3\text{-OH}$ groups in
191 lizardite ($x = 0$). In theory, only the transverse mode (TO) is IR active for infinite crystals.
192 However when crystals exhibit one (or more) dimension much smaller than the wavelength of the
193 IR radiations ($0.78 - 1000 \mu\text{m}$), both the LO and TO modes are observed (Farmer 1998; Balan et
194 al. 2002; Prencipe et al. 2009). Therefore the wavenumber of the observed IR bands are strongly
195 dependent on the lizardite particles size. Similar lizardites were synthesized and exhibited
196 essentially small rounded particles with 40 nm in diameter and few lathed particles with $0.2 \mu\text{m}$
197 in length (Mondésir and Decarreau 1987). So, for lizardite ($x = 0$), the bands at 3698 and 7226
198 cm^{-1} and the shoulders at 3688 and 7203 cm^{-1} possibly correspond to the LO-TO splitting of the
199 Mg_3OH groups (Farmer 1998; Prencipe et al. 2009).

200 **The OH combination bands.** In the $3850 - 4500 \text{ cm}^{-1}$ region, the lizardite ($x = 0$)
201 spectrum exhibited two main bands located at 4305 and 4275 cm^{-1} while for nepouite ($x = 3$),
202 only one main asymmetric broad band was observed at 4280 cm^{-1} (Fig. 5). In the 4500 and 5000
203 cm^{-1} region (Fig. 5) two bands at 4780 and 4709 cm^{-1} were observed in the lizardite ($x = 0$)
204 spectrum, which shifted with increasing Ni contents to 4722 and 4650 cm^{-1} , respectively.

205 **Origins of combination bands for lizardite ($x = 0$) and nepouite ($x = 3$) end members.**

206 The combination bands due to water ($5000 - 5500 \text{ cm}^{-1}$) are well known for clay minerals
207 (Cariati et al. 1981, 1983a; b). But the observed combination bands in the $3850 - 5000 \text{ cm}^{-1}$ range
208 are generally not assigned, except for the combination bands arising from combination of
209 stretching and bending structural OH groups for some clay minerals (Frost et al. 2002; Gates
210 2008; Bishop et al. 2008; Andrieux and Petit 2010; Madejová et al. 2011; Petit et al. 2015).

211 The wavenumber of observed combination bands was measured for both lizardite ($x = 0$)
212 and nepouite ($x = 3$) end-members using the second derivative treatment of spectra (Fig. 7.a for
213 lizardite ($x = 0$) and Fig. 7.b for nepouite ($x = 3$)). Generally in infrared spectroscopy, the signal
214 treatment like the second derivative is more suitable to reveal the band position than the
215 decomposition process, due to the relatively broad and complex bands (Gionis et al. 2006;
216 Chryssikos et al. 2009). The 21 observed features (Fig. 7) were listed in Table 1 for lizardite ($x =$
217 0) and in Table 2 for nepouite ($x = 3$).

218 Absorption bands in the combination region result from the sharing of IR radiation energy
219 between two or more fundamental vibrations which are observed in MIR range (Ciurczak 2006).
220 Consequently, a second derivative treatment was realized on MIR spectra of each end-members
221 in order to reveal the position of MIR features (Fig. 8.a for lizardite ($x = 0$) and Fig. 8.b for
222 nepouite ($x = 3$)). First, all combinations between one νOH and one lattice or δOH bands were
223 calculated (Table 3.a for lizardite ($x = 0$) and Table 3.b for nepouite ($x = 3$)). The wavenumber of
224 the combination band corresponds then more or less to the summation of the wavenumber of the
225 implicated vibrations. The proposed attribution of bands was made using a difference limit (Δ)
226 arbitrary fixed at 10 cm^{-1} between calculated and observed NIR band positions (Table 1 and 2).
227 This relatively high limit value is assumed to be due to the shift which could result from the
228 actual position of a band and the position of the band determined by the second derivative of NIR
229 and MIR spectra. The difference limit is also assumed to include a possible contribution of
230 anharmonicity.

231 Most of the bands observed in the NIR spectra of lizardite ($x = 0$) (Table 1) and nepouite
232 ($x = 3$) (Table 2) can be explained by the summation of two MIR bands (bands # 1, 3 to 12, 14,
233 and 19 to 21 for lizardite ($x = 0$) and bands # 1 to 9, 11 to 13, and 19 to 21 for nepouite ($x = 3$)).
234 Some of them could have several origins (bands # 6, 7, 9, and 19 for lizardite ($x = 0$) and bands #

235 2, 4 to 7, and 11 for nepouite ($x = 3$)). For nepouite ($x = 3$), the proximity between NIR bands (14
236 cm^{-1} between bands # 8 and 9; and 15 cm^{-1} between bands # 5 and 6), did not allow to
237 discriminate between the two possible combinations (e.g. bands # 8 and 9 and bands # 5 and 6,
238 respectively - Table 2).

239 A rather good agreement is observed between the experimental NIR spectra and the
240 calculated NIR band positions for both lizardite ($x = 0$) and nepouite ($x = 3$). But some of the
241 observed NIR bands remained unexplained (# 2, 13, 15 to 18 for lizardite ($x = 0$) and # 10, 14 to
242 18 for nepouite ($x = 3$)). The band # 2 in lizardite ($x = 0$) spectrum cannot be explained by any
243 combination within the fixed difference limit (Δ). However, this band is at an intermediate
244 position between NIR bands # 1 and 3 and then could result from an overlap of these two bands.
245 Such an overlap may generate a broad band centered at the position of the observed band # 2.

246 Note that some of the calculated combinations (Table 3) were not observed on the NIR
247 spectra of both end-members. These combinations may be forbidden and are not valid or maybe
248 of too low intensity and hidden by another band.

249 When it was possible to identify the MIR features corresponding to a same vibrational
250 group in both lizardite ($x = 0$) and nepouite ($x = 3$) end-members spectra, they were labelled with
251 the same letter (a to i - Fig. 8). The attribution of NIR combinations was then compared between
252 both end-members (Table 4). The combination bands concerning equivalent vibrational groups
253 for lizardite ($x = 0$) and nepouite ($x = 3$) spectra give confidence on the attribution of the
254 observed NIR combination bands.

255 In both end-member spectra, some bands between 4300 and 4600 cm^{-1} could not be
256 explained by combinations between two MIR features. Combinations with three MIR features
257 were tested (Supplementary files b and c for lizardite ($x = 0$) and nepouite ($x = 3$), respectively)
258 to tentatively attribute the observed NIR bands in the $4300 - 4600 \text{ cm}^{-1}$ range. Many

259 combinations between three MIR features could explain the observed NIR bands which were not
260 attributed previously. These combinations between three MIR features could correspond to
261 combinations between one MIR feature and one NIR feature (previously attributed; Table 1 and
262 2) localized in the low wavenumbers range of NIR spectra ($3850 - 4300 \text{ cm}^{-1}$).

263 To simplify the attribution of observed NIR bands for both end-members and to reduce
264 the error of position, combinations between one MIR feature with one observed NIR feature in
265 the low wavenumbers range of the NIR spectra were made (Table 5 for lizardite ($x = 0$) and
266 Table 6 for nepouite ($x = 3$)). The bands # 13, 15, 16, 17, and 18, in the lizardite ($x = 0$) spectrum
267 and bands # 14, 15, 16, 17, and 18, in the nepouite ($x = 3$) spectrum, could be explained by
268 several combinations with one MIR and one NIR features. Note that the bands observed in the
269 $4300 - 4600 \text{ cm}^{-1}$ range could not be explained by combinations of two MIR features (Table 1 and
270 2 for lizardite ($x = 0$) and nepouite ($x = 3$), respectively) but they could be explained by
271 combinations with three MIR features. More precisely, all these bands could be explained by
272 combinations between observed NIR features in the low wavenumbers range of the NIR spectra
273 and the MIR band noted c (at 401 cm^{-1} for lizardite ($x = 0$) and at 379 cm^{-1} for nepouite ($x = 3$),
274 Fig. 8). The origin of this MIR band noted c, was not found in the literature as far as the authors
275 are aware. The complex pattern of IR spectra in the $400 - 200 \text{ cm}^{-1}$ was assumed to involve mixed
276 vibrations involving the silicon-oxygen network, the octahedral cations and the hydroxyl group
277 (Farmer 1974).

278

279

Implications

280 NIR spectroscopy is widely used for remote-sensing and field studies to identify clay
281 minerals. However, NIR spectra are often complex and uninterpreted even for monomineral
282 samples, especially in the combination region where the origin of bands is unknown for many

283 clay minerals. Substantial progress in the interpretation of the IR spectra can be realized from
284 chemical series of monomineral samples with controlled distribution of atoms. Hydrothermal
285 syntheses allowed to obtain those chemical series. In this paper, samples from the lizardite-
286 nepouite series with a random distribution of Ni and Mg were synthesized to obtain robust
287 reference spectra. Because the $2\nu R^{2+}_3\text{-OH}$ vibrations were attributed, these reference spectra
288 could be used in field geology to discriminate the Ni distribution in single phase or in intimate
289 mixture between 1:1 (lizardite-nepouite) and 2:1 (kerolite-pimelite) phyllosilicates from lateritic
290 nickel ore deposits as in garnierite. Note that the $2\nu\text{OH}$ in NIR region provided more resolved
291 features compared to the νOH in MIR region and may help to distinguish between the 1:1 and the
292 2:1 Mg-Ni phyllosilicates even if partial overlapping of bands (Fig. 9).

293 The bands observed in the combination region were attributed with confidence by
294 comparing both lizardite ($x = 0$) and nepouite ($x = 3$) spectra. The observed combination bands
295 result from combinations of two or three MIR features. Those combined MIR features can result
296 from the same vibrational group (e.g. combination between δOH and νOH vibrations) or from
297 different vibrational groups (e.g. combination between νOH and $\nu\text{Si-O}$ vibrations). The work of
298 interpretation by analogy using chemical series is essential for aiding the interpretation of IR
299 spectra. Indeed calculations of theoretical spectra (e.g. Balan et al. 2002; Prencipe et al. 2009)
300 cannot be performed up to now for minerals which contain transition metals (e.g. Ni, Fe...).

301

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306

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447 **Figure captions:**

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449 **Figure 1.** Powder XRD patterns of synthesized lizardite-nepouite series ($\text{Si}_2\text{Mg}_{3-x}\text{Ni}_x\text{O}_5(\text{OH})_4$).

450

451 **Figure 2.** XRD patterns of (06-33) reflections of synthesized lizardite-nepouite series ($\text{Si}_2\text{Mg}_{3-x}$
452 $\text{Ni}_x\text{O}_5(\text{OH})_4$).

453

454 **Figure 3.** $d(06-33)$ values (\AA) versus Ni content (x) in lizardite-nepouite synthetic series ($\text{Si}_2\text{Mg}_{3-x}$
455 $\text{Ni}_x\text{O}_5(\text{OH})_4$). The size of symbol denotes the error on the $d(06-33)$ measurements.

456

457 **Figure 4.** Selected regions of the MIR spectra of synthesized lizardite-nepouite series ($\text{Si}_2\text{Mg}_{3-x}$
458 $\text{Ni}_x\text{O}_5(\text{OH})_4$).

459

460 **Figure 5.** Selected regions of the NIR spectra of synthesized lizardite-nepouite series ($\text{Si}_2\text{Mg}_{3-x}$
461 $\text{Ni}_x\text{O}_5(\text{OH})_4$).

462

463 **Figure 6.** Wavenumbers of the ν OH bands versus wavenumbers of the 2ν OH first overtones for
464 the synthesized lizardite-nepouite samples - this study (\bullet), for various OH groups in talc (\square and
465 Ni-Mg \blacksquare) (Petit et al. 2004) and for palygorskite (Δ) (Gionis et al. 2006). The size of symbols
466 denotes the error on the wavenumber measurements.

467

468 **Figure 7.** NIR spectra in the combination region and their second derivative of lizardite ($x = 0$)
469 ($\text{Si}_2\text{Mg}_3\text{O}_5(\text{OH})_4$) (a), and nepouite ($x = 3$) ($\text{Si}_2\text{Ni}_3\text{O}_5(\text{OH})_4$) (b). Numbers 1 to 21 correspond to

470 combination bands listed in table 1 for lizardite ($x = 0$) and in table 2 for nepouite ($x = 3$). In
471 grey, combination band positions from the second derivative NIR spectra.

472

473 **Figure 8.** Second derivative of MIR spectra of lizardite ($x = 0$) ($\text{Si}_2\text{Mg}_3\text{O}_5(\text{OH})_4$) (a), and
474 nepouite ($x = 3$) ($\text{Si}_2\text{Ni}_3\text{O}_5(\text{OH})_4$) (b). Letters correspond to the same vibrational group for each
475 end-member.

476

477 **Figure 9.** First OH-overtone ($2\nu\text{OH}$) region of synthesized Ni-lizardite ($\text{Si}_2\text{Mg}_{1.5}\text{Ni}_{1.5}\text{O}_5(\text{OH})_4$)
478 and Ni-kerolite ($\text{Si}_4\text{Mg}_{1.5}\text{Ni}_{1.5}\text{O}_{10}(\text{OH})_2 \cdot n\text{H}_2\text{O}$).

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494 **Tables:**

495

496 Table 1. Observed NIR combination band positions of lizardite ($x = 0$) and calculated NIR
 497 combination band positions from combination with two MIR features. Δ corresponds to the
 498 difference between the calculated and the observed combination band positions. † corresponds to
 499 small identified features (see Fig. 7a).

Band #	Observed NIR bands (cm ⁻¹)	Combination with two MIR features (cm ⁻¹)			Calculated NIR bands (cm ⁻¹)	Δ (cm ⁻¹)	
1	3958	302	+	3648	=	3950	8
2	3985						
3	4001	302	+	3695	=	3997	4
4	4032	380	+	3648	=	4028	4
5†	4049†	401	+	3648	=	4049	0
6	4077	380	+	3695	=	4075	2
		434	+	3648	=	4082	5
7	4121	434	+	3695	=	4129	8
		481	+	3648	=	4129	8
8	4163	458	+	3695	=	4153	10
9	4199	504	+	3695	=	4199	0
		554	+	3648	=	4202	3
10†	4240†	554	+	3695	=	4249	9
11	4274	635	+	3648	=	4283	9
12	4307	607	+	3695	=	4302	5
13	4363						
14†	4396†	693	+	3695	=	4388	8
15	4409						
16	4442						
17†	4487†						
18†	4531†						
19	4675	974	+	3695	=	4669	6
		1024	+	3648	=	4672	3
20	4709	1024	+	3695	=	4719	10
21	4781	1086	+	3695	=	4781	0

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501

502 Table 2. Observed NIR combination band positions of nepouite ($x = 3$) and calculated NIR
 503 combination band positions from combination with two MIR features. Δ corresponds to the
 504 difference between the calculated and the observed combination band positions. † corresponds to
 505 small identified features (see Fig. 7b).

506

Band #	Observed NIR bands (cm^{-1})	Combination with two MIR features (cm^{-1})			Calculated NIR bands (cm^{-1})	Δ (cm^{-1})	
1	3934	318	+	3608	=	3926	8
2	3971	318	+	3649	=	3967	4
		357	+	3608	=	3965	6
3	4000	357	+	3649	=	4006	6
4†	4037†	379	+	3649	=	4028	9
		427	+	3608	=	4035	2
5	4056	404	+	3649	=	4053	3
		456	+	3608	=	4064	8
6†	4071†	427	+	3649	=	4076	5
		456	+	3608	=	4064	7
7	4097	456	+	3649	=	4105	8
		493	+	3608	=	4101	4
8	4136	493	+	3649	=	4142	6
9	4150	493	+	3649	=	4142	8
10†	4182†						
11	4277	628	+	3649	=	4277	0
		676	+	3608	=	4284	7
12	4297	652	+	3649	=	4301	4
13	4321	676	+	3649	=	4325	4
14	4348						
15	4383						
16†	4426†						
17	4447						
18†	4522†						
19	4652	1049	+	3608	=	4657	5
20	4698	1049	+	3649	=	4698	0
21	4722	1079	+	3649	=	4728	6

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509 Table 3. Calculated combinations (in cm^{-1}) between νOH and lattice or δOH bands; a: for
 510 lizardite ($x = 0$) and b: for nepouite ($x = 3$).

a	lizardite ($x = 0$)		b	nepouite ($x = 3$)	
	Lattice or δOH bands	νOH bands		Lattice or δOH bands	νOH bands
	3648	3695		3608	3649
1086	4734	4781	1079	4687	4728
1024	4672	4719	1049	4657	4698
974	4622	4669	1015	4623	4664
693	4341	4388	978	4586	4627
635	4283	4330	676	4284	4325
607	4255	4302	652	4260	4301
554	4202	4249	628	4236	4277
504	4152	4199	614	4222	4263
481	4129	4176	493	4101	4142
458	4106	4153	456	4064	4105
434	4082	4129	427	4035	4076
401	4049	4096	404	4012	4053
380	4028	4075	379	3987	4028
302	3950	3997	357	3965	4006
			318	3926	3967

511

512 Table 4. Comparison of some combination bands for both lizardite ($x = 0$) and nepouite ($x = 3$)
 513 end-members. Letters correspond to MIR features which correspond to the equivalent vibrational
 514 groups for each end-member. † corresponds to small identified features (see Fig. 7).

lizardite ($x = 0$)		Combinations from equivalent vibrational groups	nepouite ($x = 3$)	
Band #	Observed NIR bands (cm^{-1})		Observed NIR bands (cm^{-1})	Band #
1	3958	a + h	3934	1
3	4001	a + i	3971	2
4	4032	b + h		
6	4077	b + i	4000	3
		d + h	4037†	4†
7	4121	d + i	4071†	6†
8	4163	e + i	4097	7
21	4781	g + i	4722	21

515

516 Table 5. Calculated NIR combination band positions (4300 - 4800 cm^{-1}) for lizardite ($x = 0$) from
 517 combination with one MIR feature and one NIR feature. Δ corresponds to the difference between
 518 the calculated and the observed combination band positions. *in letter in MIR spectra (Fig. 8) and
 519 in integer in NIR spectrum (Fig. 7). † corresponds to small identified features (see Fig. 7a).

520

Band #	Observed NIR bands (cm^{-1})	Combination with one MIR band and one NIR band (cm^{-1})				Calculated NIR bands (cm^{-1})	Δ (cm^{-1})	Observed features involved*
13	4363	380	+	3985	=	4365	2	b ; 2
		401	+	3958	=	4359	4	c ; 1
15	4409	380	+	4032	=	4412	3	b ; 4
		401	+	4001	=	4402	7	c ; 3
		434	+	3985	=	4419	10	d ; 2
		458	+	3958	=	4416	7	e ; 1
16	4442	401	+	4032	=	4433	9	c ; 4
		401	+	4049	=	4450	8	c ; 5
		434	+	4001	=	4435	7	d ; 3
		458	+	3985	=	4443	1	e ; 2
		481	+	3958	=	4439	3	-
17†	4487†	401	+	4077	=	4478	9	c ; 6
		434	+	4049	=	4483	4	d ; 5
		458	+	4032	=	4490	3	e ; 4
		481	+	4001	=	4482	5	-
		504	+	3985	=	4489	2	-
18†	4531†	401	+	4121	=	4522	9	c ; 7
		458	+	4077	=	4535	4	e ; 6
		481	+	4049	=	4530	1	-
		504	+	4032	=	4536	5	-
		554	+	3985	=	4539	8	-

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525

526 Table 6. Calculated NIR combination band positions (4300 - 4800 cm^{-1}) for nepouite ($x = 3$) from
 527 combination with one MIR feature and one NIR feature. Δ corresponds to the difference between
 528 the calculated and the observed combination band positions. *in letter in MIR spectra (Fig. 8) and
 529 in integer in NIR spectrum (Fig. 7). † corresponds to small identified features (see Fig. 7b).

Band #	Observed NIR bands (cm^{-1})	Combination with one MIR band and one NIR band (cm^{-1})				Calculated NIR bands (cm^{-1})	Δ (cm^{-1})	Observed features involved*
14	4348	318	+	4037	=	4355	7	a ; 4
		357	+	4000	=	4357	9	b ; 3
		379	+	3971	=	4350	2	c ; 2
		404	+	3934	=	4338	10	d ; 1
15	4383	318	+	4056	=	4374	9	a ; 5
		318	+	4071	=	4389	6	a ; 6
		379	+	4000	=	4379	4	c ; 3
		404	+	3971	=	4375	8	-
16†	4426†	456	+	3934	=	4390	7	e ; 1
		357	+	4071	=	4428	2	b ; 6
		379	+	4037	=	4416	10	c ; 4
		379	+	4056	=	4435	9	c ; 5
		427	+	4000	=	4427	1	d ; 3
17	4447	456	+	3971	=	4427	1	e ; 2
		493	+	3934	=	4427	1	-
		318	+	4136	=	4454	7	a ; 8
		357	+	4097	=	4454	7	b ; 7
		379	+	4071	=	4450	3	c ; 6
18†	4522†	404	+	4037	=	4441	6	-
		456	+	4000	=	4456	9	e ; 3
		379	+	4136	=	4515	7	c ; 8
		379	+	4150	=	4529	7	c ; 9
		427	+	4097	=	4524	2	d ; 7
		456	+	4056	=	4512	10	e ; 5
18†	4522†	456	+	4071	=	4527	5	e ; 6
		493	+	4037	=	4530	8	-

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