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**Collapsing minerals: Crackling noise of sandstone and coal, and  
the predictability of mining accidents**

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**ABSTRACT**

Mining accidents are sometimes preceded by high levels of crackling noise which follow universal rules for the collapse of minerals. The archetypal test cases are sandstone and coal. Their collapse mechanism is almost identical to earthquakes: the crackling noise in large, porous samples follows a power law (Gutenberg-Richter) distribution  $P \sim E^{-\epsilon}$  with energy exponents  $\epsilon$  for near critical stresses of  $\epsilon = 1.55$  for dry and wet sandstone, and  $\epsilon = 1.32$  for coal. The exponents of early stages are slightly increased, 1.7 (sandstone) and 1.5 (coal), and appear to represent the collapse of

22 isolated, uncorrelated cavities. A significant increase of the acoustic emission, AE,  
23 activity was observed close to the final failure event, which acts as ‘warning signal’ for  
24 the impending major collapse. Waiting times between events also follow power law  
25 distributions with exponents  $2+\xi$  between 2 and 2.4. Aftershocks occur with  
26 probabilities described by Omori coefficients  $p$  between 0.84 (sandstone) and 1 (coal).  
27 The ‘Båth’s law’ predicts that the ratio between the magnitude of the main event and  
28 the largest aftershock is 1.2. Our experimental findings confirm this conjecture.  
29 Our results imply that acoustic warning methods are often possible within the context  
30 of mining safety measures but that it is not only the increase of crackling noise which  
31 can be used as early warning signal but also the change of the energy distribution of the  
32 crackling events.

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34 **KEYWORDS:** Sandstone, coal, crackling noise, failure and collapse event, precursor  
35 effects.

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## INTRODUCTION

38 Earthquakes and the collapse of porous materials are related phenomena deeply  
39 connected by the emission of crackling noise (Baró et al. 2013; Salje and Dahmen 2014;  
40 Sethna et al. 2001) where systems under slow perturbation respond through discrete  
41 events, so-called ‘jerks’, with a huge variety of sizes and energies. The signatures of  
42 seismic events in geophysics coincide with laboratory-scale experiments (‘labquakes’)  
43 of compressed porous and fractured materials (Davidsen et al. 2007; Diodati et al.  
44 1991; Hirata 1987; Kun et al. 2007, 2009; Lebyodkin et al. 2013; Nataf et al. 2014a;  
45 Niccolini et al. 2009, 2010, 2011; Petri et al. 1994; Salje et al. 2013; Weiss and Miguel  
46 2004) and have been simulated by numerical discrete element calculations of porous  
47 materials (Kun et al. 2013, 2014). In laboratory experiments, external loading is applied  
48 to the samples and the system’s response is obtained by recording acoustic emission  
49 (AE). Other recordings are the stepwise change of the macroscopic strain or the  
50 emission of calorimetric heat jerk (Baró et al. 2014; Gallardo et al. 2010). All  
51 recordings mimic earthquakes since the main stresses underlying tectonic quakes are  
52 considered compressive and stationary (Main 1996). Baró et al. (2013) reported a very  
53 complete parallel between the acoustic emissions produced by a porous material under  
54 uniaxial compression and earthquakes. The same experimental techniques are widely  
55 used for the investigation of device materials such as ferroelectric, ferromagnets, and  
56 ferroelastics (Bolgár et al. 2016; Dul’kin et al. 2015; Guyot et al. 1988; Hoffmann et al.  
57 2001; Salje et al. 2014, 2015; Skal's'kyi et al. 2009; Vives et al. 1994) with a significant

58 increase of published data over recent years on the acoustic emission during  
59 force-induced changes of microstructures.

60

61 Previous experimental studies of labquakes have given some evidence that major  
62 collapse events are preceded by increased precursor crackling noise, which may allow  
63 the prediction of failure during earthquakes. Equally importantly, predicting failure is  
64 needed in the mining context. The main question is then: is it possible to predict a main  
65 collapse event from pre-shocks before the failure event actually occurs? First  
66 observations of large-scale foreshock sequences go back to 1988 were a full sequence  
67 was observed at the Chalfat earthquake by Smith and Priestley (1988) and large  
68 sequences of Californian earthquakes by Dodge et al. (1996). In each case the statistical  
69 evidence was rather limited and related to technical issues of seismological  
70 observations. More complete data from laboratory experiments, such as from  
71 observations in porous goethite, FeO(OH), revealed two scenarios (Salje et al. 2013).  
72 Samples with low porosity showed no evidence for any precursor effects and no ‘early  
73 warning’ signal could be extracted from the compression noise. Samples with high  
74 porosities ( > 80%), on the other hand, did show precursor noise and opened the  
75 possibility to use pico-seismic observations to predict the collapse of a goethite mine  
76 (Salje et al. 2013). Subsequent work found no indication of increased crackling noise in  
77 berlinite (Nataf et al. 2014b). Instead there was an indication that the exponent of  
78 power-law energy distribution reduces near the critical point, in agreement with trends

79 in numerical simulations of collapse mechanisms by Kun et al. (2013).  
80 No significant increase of the AE activity was observed in the first such study of  
81 SiO<sub>2</sub>-based vycor (Salje et al. 2011) while an extensive study of other SiO<sub>2</sub> based  
82 materials found only a very weak increase of precursor activity in sandstone (Nataf et  
83 al. 2014a). No effect was found in charcoal (Ribeiro et al. 2015). These results  
84 contradict the simulation results (Kun et al. 2013) where both a big increase of AE  
85 activity and a change of the power law exponent were predicted. To test this scenario  
86 we changed the experimental arrangement from very small load stresses and samples  
87 (Salje et al. 2011) to one where much larger samples can be compressed under  
88 enhanced forces. This novel experimental arrangement allows us to study  
89 systematically the major collapse mechanisms in the mineralogical context.

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## **EXPERIMENTAL**

92 The samples of sandstone and coal were collected from the Sichuan and Shanxi  
93 provinces of China. The samples were drilled with a high speed rotary saw from larger  
94 blocks, their shapes were cylindrical with 50 mm diameter and 100 mm length. The  
95 sides of the specimen were optically smooth, and the ends of the specimens were  
96 smooth within  $\pm 0.02$ mm (according to ISRM testing guidelines, Fairhurst and Hudson  
97 1999). The density and porosity were determined by wax seal methods and mercury

98 intrusion analysis, respectively. They are very similar to those of smaller samples  
99 measured previously (Table 1)

100 Dry sandstone samples were heated to 110°C for 24h, and cooled to room temperature  
101 just before the compression experiment. Saturated sandstones were immersed in water  
102 for 48h.

103

104 The compression experiment was performed using the loading equipment in Figure 1.  
105 The slowly increasing load is provided by oil pouring into a container at a constant flow  
106 rate, the weight of oil is then transferred to the lower tilting beam in Figure 1. The  
107 samples were placed between the lower tilting beam and a static support. The  
108 maximum load is 300 kN and the maximum vertical displacement is 5mm. The stress  
109 rate was chosen to be  $d\sigma/dt = 8.5\text{kPa/s}$  (1kN/min) for all samples.

110

111 Acoustic emission signals were measured during compression by two or more  
112 piezoelectric sensors (NANO-30 Physical Acoustics Company) fixed on the sample's  
113 round surface by rubber bands. The sensors were acoustically coupled to the sample by  
114 a thin layer of grease. The acoustic signal was pre-amplified (40 dB) and transferred to  
115 the AE analysis system (DISP from American Physical Acoustics Company). The  
116 threshold for detection was chosen as the signal of an empty experiment (45 dB).

117

118

## RESULTS

119 The energy of the AE signal, the AE activity (the number of AE hits per second), and  
120 the cumulative AE activity are shown as function of the run time in Figure 2 for (a) dry  
121 sandstone, (b) wet sandstone and (c) coal. Note the logarithmic scale for the event  
122 energies which spans up to 4 decades. AE energies and activities are smaller in the early  
123 stages of the compression experiment compared with the late stages. The AE emission  
124 reaches a steady state in coal which is terminated before the final major failure event.  
125 Some early signals come from the friction between sample's flat faces and the  
126 compressive equipment, and the closure of some original micro-cracks in the samples.  
127 The AE signals increase dramatically near the major failure event, most notably in  
128 sandstone samples, where virtually no steady state emission occurs.

129

130 The density and porosity of our sandstone samples are close to those of Nataf et al.  
131 (2014a, see Table 1), although our failure stress is about 5 times higher than theirs (see  
132 Table 2). This may be due to our faster loading rates (Table 2), and smaller levels of  
133 stress concentrations in our cylindrical samples compared with the previously used  
134 prismatic samples. Our sandstone is also particularly uniform with few preexisting  
135 cracks which leads to fewer AE events during the middle stage (Figure 2). Coal  
136 contains more original micro cracks than sandstone and more AE signals were recorded  
137 before failure.

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## ANALYSIS

140 **The energy distribution (Gutenberg-Richter law)**

141 The probability distribution function, PDF, of jerk energies (events) is  $P(E)$  and is  
142 derived from the raw data by appropriate linear binning of the event energies. The  
143 number of bins was chosen between  $10^4$  and  $10^6$  with little influence of the bin number  
144 on the functional form of the PDF. Logarithmic binning did not change the results.  
145 Figure 3 shows the energy distributions  $P(E)$  in log-log plots for dry and wet sandstone,  
146 and coal. The histogram corresponds to the accumulation of signals along the whole  
147 experiment. A good power law behavior is observed over more than three decades for  
148 the early stages and late stages of each collapse sequence: that the distribution of  
149 energies follows a power law (Gutenberg-Richter law)  $P(E) \sim E^{-\varepsilon}$  is a very good  
150 approximation but with different exponents for each data set. A finer sequencing with 5  
151 intervals in the early stages and 3 intervals for the late stages lead to the same result,  
152 namely that the exponents show only two different numerical values with a larger value  
153 at the early stages and the smaller value near the major failure event. In each case, the  
154 distribution is described by

155 
$$P(E)dE \sim \frac{E^{-\varepsilon}}{E_{min}^{1-\varepsilon}} dE \quad E > E_{min} \quad (1)$$

156 where  $E_{min}$  is a lower cutoff used for normalization. To examine the distribution in more  
157 detail we apply the Maximum Likelihood method (Clauset et al. 2009). This method  
158 avoids the construction of histograms and the choice of the number of bins. The  
159 analytical formula is

160 
$$\varepsilon(x_{min}) = 1 + n \left[ \sum_{i=1}^n \ln \frac{x_i}{x_{min}} \right]^{-1} \quad (2)$$

161 where  $x_i$ ,  $i = 1 \dots n$  are the observed values of  $x$  such that  $x_i \geq x_{\min}$ .

162 The standard error is

$$163 \quad \sigma = \frac{\varepsilon(x_{\min})^{-1}}{\sqrt{n}} + O\left(\frac{1}{n}\right) \quad (3)$$

164 The results are as shown in the inserts of Figure 3, this analysis leads to a plateau which

165 defines the exponential parameter  $\varepsilon$ . Note that we define  $\varepsilon$  as a positive quantity, the

166 negative sign in the exponent then defines the negative slope of the power law curve.

167 As the number of data points at the late stages (blue curves in the inserts) is much

168 greater than in the early stages we find a much better defined plateau in this case with

169 well-defined exponents  $\varepsilon \approx 1.55$  (sandstone) and  $\varepsilon \approx 1.32$  (coal) (Figure 4). The

170 agreement between the two methods, namely direct binning and the Maximum

171 Likelihood, for the determination of  $\varepsilon$  is excellent.

172

### 173 **Distribution of waiting times**

174 Figure 5 shows the distribution of waiting times, defined as  $\delta_j = t_j - t_{j-1}$ , with  $j$  labeling

175 only the events with energy larger than a given threshold energy  $E_{\min}^*$ .  $D(\delta, E_{\min}^*)$  is the

176 waiting time distribution function and indicates the probability to observe a waiting

177 time  $\delta$  for a threshold energy  $E_{\min}^*$ . When plotting  $D(\delta, E_{\min}^*)$  as function of  $\delta$ , we scale

178 the axes as  $\langle r(E_{\min}^*) \rangle \delta$  and  $D(\delta, E_{\min}^*) / \langle r(E_{\min}^*) \rangle$ , where  $\langle r(E_{\min}^*) \rangle$  is the mean

179 number of events per unit time with an energy  $E > E_{\min}^*$ . This approach leads to a

180 collapse of all data in a single curve showing double power-law behavior with

181 exponents  $1 - \nu$  for small arguments, and  $2 + \xi$  for large arguments (we follow again the

182 convention to define the exponents as positive quantities and maintain the negative sign  
183 to indicate the negative slope of the power law function). We have insufficient data to  
184 determine  $(1 - \nu)$  while the results for  $(2 + \xi) = 2.2 \pm 0.2$  are sufficiently well  
185 constrained for all data sets. No significant change of  $(2 + \xi)$  was found between dry  
186 and water-saturated sandstone.

187

### 188 **Aftershocks and Båth's law**

189 The number of aftershocks (AS) is described by the Omori's law (Utsu et al. 1995) as  
190 often employed for the analysis of earthquakes. It states that the number of AS decays  
191 as a power-law after each mainshock (MS). We define MS as AE signals with energies  
192  $E_{MS}$  between  $10^k$  to  $10^{k+1}$  aJ, with  $k = 1, 2,$  and  $3$ . The sequence of AS is then continued  
193 until another MS is found, which terminates the AS sequence. We calculate the  
194 aftershock rates as function of the lapse time since the MS. The results of dry sandstone,  
195 wet sandstone, and coal are shown in Figure 6 (a)–(c). The power law dependence is  
196 emphasized by the averaged slope with Omori exponents  $p=0.84$  (sandstone) and  
197  $p=0.95$  (coal). These values are typical for Omori sequences in natural earthquakes.

198

199 The Båth's law (Båth 1965; Console et al. 2003; Helmstetter and Sornette 2003) states  
200 that the ratio of the energy magnitudes of a MS and a AS is, on average, near to 1.2.  
201 This ratio is independent of the magnitude of the MS.

202 We plot in Figure 7 the normalized ratio between the magnitude of the mainshock MS  
203 and its largest aftershock AS\*

$$204 \quad \Delta M = \log \left( \frac{E_{MS}}{E_{AS}^*} \right) \quad (4)$$

205 as function of the magnitude of MS. The ratio  $\Delta M$  shows indeed a trend towards the  
206 value of the Båth's law of 1.2 for large MS. The dependency of  $\Delta M$  on the magnitude of  
207 the main shock is well described by extended Debye model:

$$208 \quad \Delta M = A_2 + \frac{(A_1 - A_2)}{1 + \left(\frac{E_{MS}}{E_0}\right)^p} \quad (5)$$

209  $A_1=0.13$ ,  $A_2=1.16$ ,  $E_0=413.65$ ,  $p=1.21$ , and R-square = 0.97.

210

## 211 **DISCUSSION**

212 Our investigations represent a significant advancement with respect to previous  
213 experimental studies of collapsing porous materials because we use large sample  
214 volumes and high applied stresses. These conditions are closer to those in the context of  
215 mining or the collapse of monuments than previous studies (Baró et al. 2013, 2014;  
216 Castillo-Villa et al. 2013; Gallardo et al. 2010; Nataf et al. 2014a, 2014b; Salje et al.  
217 2008, 2009, 2011, 2013; Soto-Parra et al. 2015). The large sample volume leads to a  
218 new phenomenon which was not possible to observe in small sample, which is the  
219 evolution of the event centers during the experiment. The results indicate that all  
220 avalanche characteristics can be divided into two groups, namely those at the early  
221 stages and those closer to the main failure event. Using eight AE detectors and standard

222 localization software, we determine the distribution of event centers where AE jerks  
223 originate in the sample. These distributions are shown in Figure 8.

224

225 The initial stages are characterized by randomly distributed event centers with large  
226 distances between them. The events are hence approximately randomly distributed in  
227 time and space. We describe these events as ‘uncorrelatated’. With increasing number  
228 of defect centers we find an accumulation of event centers along the shear diagonal  
229 which characterizes the final failure of the sample. The event centers are now very  
230 densely located and spatially correlated. The energy exponents for the randomly  
231 distributed events are generally larger than those of the correlated events although the  
232 difference is small. The difference between the exponents given in Table 3 are not  
233 visible in most other experiments while our high resolution investigations make it  
234 possible to distinguish between exponents within error margins of  $\delta\varepsilon = 0.1$ .

235

236 The power law exponents near the major collapse event (1.54 and 1.32) are similar to  
237 those reported by Nataf et al. (2014a) who found exponents  $\varepsilon$  between 1.44 and 1.55 for  
238 three different kinds of sandstone. Furthermore, the exponents of stage 2 for coal  
239 ( $\varepsilon_2=1.32$ ) are also compatible with the statistical results come from ethanol-dampened  
240 charcoal (1.27-1.33) (Ribeiro et al. 2015). These observations suggest that our results  
241 are consistent with previous research while the exponents for stage 1 are not only  
242 higher than the value of the correlated stage, but also higher than the results

243 of previous research. A solution to this conundrum may stem from recent results of  
244 Kun et al. (2013, 2014) who investigated cracking noise generated by failure in porous  
245 materials by computer simulation. A most remarkable feature of their results is that the  
246 value of their exponent  $\epsilon$  did not show fix-point behavior but smoothly decreased  
247 during compression. The smallest value of  $\epsilon$  was found near the final collapse. This  
248 simulation result is similar to the evolution of the exponent in this study. Our results  
249 suggest that we do not have a smooth time dependence of  $\epsilon$  but a stepwise behavior  
250 between two fix points, however. Only the second, ‘correlated’ fix point is close to the  
251 mean field solution while the first fix point may relate to uncorrelated, isolated  
252 collapses with a different collapse mechanism (Salje and Dahmen 2014). In the  
253 simulations by Kun et al. (2013), spatial positions of bursts in their sample show  
254 randomness in the early stage of compression with no memory, while damage bands are  
255 formed at the later stage. This picture is confirmed by our result in Figure 8 where first  
256 few AE centers appear in the top and bottom areas of sandstone sample (Figure 8a),  
257 then some AE centers occur randomly (Figure 8b), and finally many AE centers form  
258 the final crack (Figure 8c). This indicates that the lower energy exponent relates to  
259 ‘criticality’ near the final failure event and agrees with the observation that previous  
260 measurements on small samples lead to the same energy exponent together with a much  
261 reduced failure strength. This result can be understood if the sandstone samples of  
262 Nataf et al. (2014a) were already weakened by internal cracks so that the physical  
263 events leading to the crackling noise were intrinsically linked to correlated local failure

264 events rather than to localized collapse mechanisms as seen at the early stages during  
265 our studies.

266

267 A crossover behavior of the avalanches size was found in the study of fiber bundles and  
268 electrical fuse models (Pradhan et al. 2005). The avalanches size distributions near to  
269 and far away from the catastrophic failure follow both power law behavior with  
270 different exponents. Multiple fix-point behavior was also reported by Soto-Parra et al.  
271 (2015) for the compression of martensitic porous Ti-Ni. The first series of events is  
272 generated by de-twinning ( $\epsilon=2$ ) while later stages relate to fracture ( $\epsilon=1.7$ ). This  
273 fracture exponent is close to the early stage, uncorrelated value in our study which  
274 appears to indicate that collective shear plane failure does not occur in Ti-Ni alloys.

275

276 The waiting time distributions in Figure 5 are similar to those of previous investigations  
277 of less uniform and smaller samples. For dry and wet sandstone, the exponents  $2+\xi=2.2$   
278 and 2.4 are similar with the results for previous light-gray sandstone waiting time  
279 analysis ( $2+\xi=2.0$ ) (Nataf et al. 2014a). Exponents of  $2+\xi=2.45$  were reported for  
280 uniaxial compression of Vycor (Baró et al. 2013), a mesoporous silica ceramics. A  
281 reasonable agreement also exists with the power-law exponent  $2+\xi=2.0$  from DEM  
282 simulation (Kun et al. 2013, 2014).

283

284 Our data show an excellent adherence of the collapse sequence of sandstone to the  
285 Omori's law ( $p=0.84$  in Figure 6). Baró et al. (2013) reported a stable Omori decay in  
286 small samples with  $p=0.75$  for Vycor, and  $p=0.78$  for gray sandstone, and  $p=0.74$  for  
287 red and yellow sandstone (Nataf et al. 2014a). Coal shows an Omori behavior with  
288  $p=0.95$ , similar to charcoal ( $p=0.87$ ) (Ribeiro et al. 2015). In contrast, recent reports  
289 (Tsai et al. 2016) gave much higher values for broken bamboo chopstick and a bundle  
290 of spaghetti with  $p=1.68$  and  $p=3.53$ , respectively. The same tendency is seen for the  
291 numerical values of  $\Delta M$ .  $\Delta M$  of charcoal was reported to be 1.2 which is identical with  
292 our data. Breaking of bamboo chopsticks lead to  $\Delta M = 1.7$  and that of a bundle of  
293 spaghetti gave  $\Delta M = 0.8$  (Tsai et al. 2016). For earthquakes, large fluctuations of  $\Delta M$   
294 usually exist for different aftershock sequences (Hainzl et al. 2010).

295

296

## IMPLICATION

297 The results of our research have two major implications. Firstly, it shows that the  
298 prediction of collapse events is possible. The two indicators for an impending disaster,  
299 such as a collapse of a mining shaft or the collapse of a building, are the increase of  
300 acoustic emission of crackling noise and the change of its energy exponent. Both  
301 indicators can be measured rather easily by highly sensitive microphones attached to  
302 the material (sandstone sculptures, houses, coals seams etc). The signals need to be  
303 processed as described in this paper, which can be easily done using a simple computer  
304 device. The sensitivity of the methods depends largely on microstructural properties of

305 the minerals: uniform but porous sandstone is much more sensitive to 'early warning  
306 noise' that coal seams which contains a multitude of local cracks.  
307 Secondly, we now understand crackling noise much better because we developed a  
308 much better measurement technique which allows us to investigate very large samples.  
309 The analogy of crackling noise of porous minerals with earth quakes is now firmly  
310 established with the surprising additional feature: the energy exponent (or b-value in  
311 seismology) depends on the collectiveness of the collapse event. Local cavity collapse  
312 displays higher energy exponents than collective movements such in crack propagation  
313 and the formation of micro-faults. Only the latter is close to the theoretical mean field  
314 value. This result will doubtlessly stimulate more theoretical research in this field.

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## LIST OF TABLE AND FIGURE CAPTIONS

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502 materials (Baró et al. 2013; Nataf et al. 2014a).

503

504 **TABLE 2.** The stress rate,  $d\sigma/dt$ , failure stress,  $\sigma_f$ , number of recorded AE signals,  $N$ ,  
505 and the time span of our experiments and LGsan, Rsan, and Ysan in (Nataf et al.  
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508 **TABLE 3.** Exponents for statistical laws used in this and previous studies.

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511 into the hanging container (on the right) at a constant flow rate; the weight of oil ( $G$ ) is  
512 transferred to the lower tilting beam. The samples were placed between the lower tilting  
513 beam and a static support. (Color online.)

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523 ML-fitting exponent  $\varepsilon$  as a function of a lower threshold  $E_{\min}$ . (Color online.)

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544 (d) photo of the cracked sample. (Color online.)

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549 materials (Baró et al. 2013; Nataf et al. 2014a).

550

	Density (g/cm <sup>3</sup> )	Porosity (%)	Reference
Sandstone	2.2	0.18	This study
Coal	1.2	0.11	This study
LGsan	2.3	0.13	(Nataf et al. 2014a)
Rsan	2.2	0.17	(Nataf et al. 2014a)
Ysan	2.3	0.17	(Nataf et al. 2014a)
Vycor	1.5	0.40	(Baró et al. 2013)

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554 **TABLE 2.** The stress rate,  $d\sigma/dt$ , failure stress,  $\sigma_f$ , number of recorded AE signals,  $N$ ,  
555 and the time span of our experiments and LGsan, Rsan, and Ysan in (Nataf et al.  
556 2014a).

	$d\sigma/dt$ (kPa/s)	$\sigma_f$ (MPa)	N	T (s)	Elastic modulus (GPa)
Dry sandstone	8.5	62.2	110906	7190	6.0
Wet sandstone	8.5	46.3	21827	5477	5.8
Coal	8.5	26.4	18968	3235	1.6
LGsan	2.9	13.4	21238		
Rsan	2.4	11.0	27271		3.2
Ysan	1.4	3.6	11058		

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560 **TABLE 3.** Exponents for statistical laws used in this and previous studies.

	$\varepsilon_1/\varepsilon_2$ or $\langle \varepsilon \rangle$	$1 - \nu$	$2 + \xi$	$p$	$\Delta M$	Reference
Dry sandstone	1.77/1.53		2.2	0.84	1.2	This study
Wet sandstone	1.71/1.56		2.4	0.85	1.2	This study
Coal	1.51/1.32		2.0	0.95	1.2	This study
LGsan	$\langle 1.48 \rangle$	0.86	2.0	0.78		(Nataf et al. 2014a)
Rsan	$\langle 1.55 \rangle$	1.12	2.3	0.74		(Nataf et al. 2014a)
Ysan	$\langle 1.49 \rangle$	1.01	1.8	0.74		(Nataf et al. 2014a)
Vycor	$\langle 1.39 \rangle$	0.93	2.45	0.75		(Baró et al. 2013)
Charcoal	$\langle 1.3 \rangle$			0.87	1.2	(Ribeiro et al. 2015)
Cu-Zn-Al alloys	$\langle 2.15 \rangle$	0.9	2.2			(Baró et al. 2014)
Bamboo	$\langle 1.45 \rangle$			1.68	1.7	(Tsai et al. 2016)
Spaghetti	$\langle 1.35 \rangle$			3.53	0.8	(Tsai et al. 2016)
Simulation	$\langle 2.02 \rangle$		2.0			(Kun et al. 2014)

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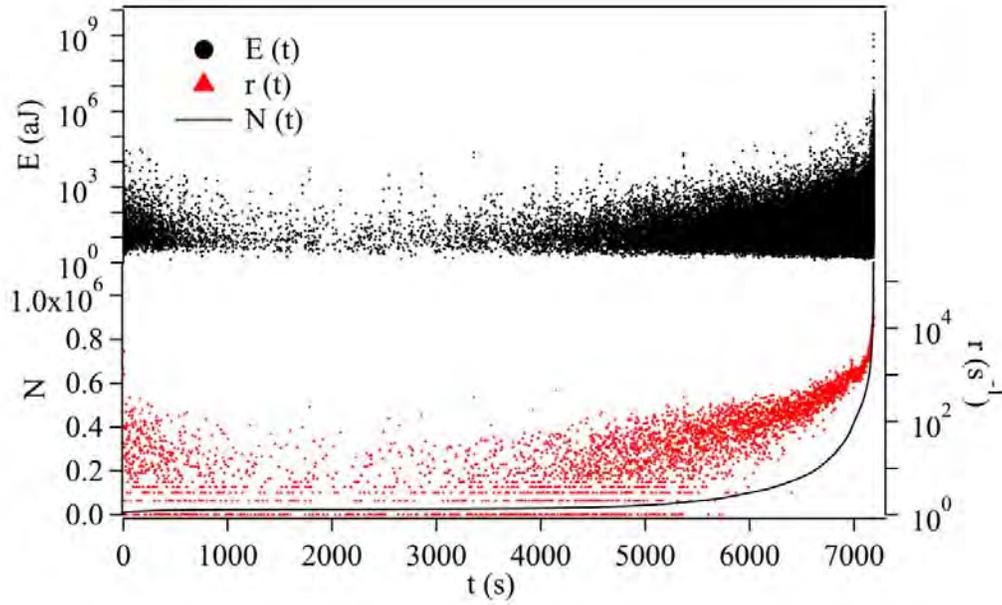
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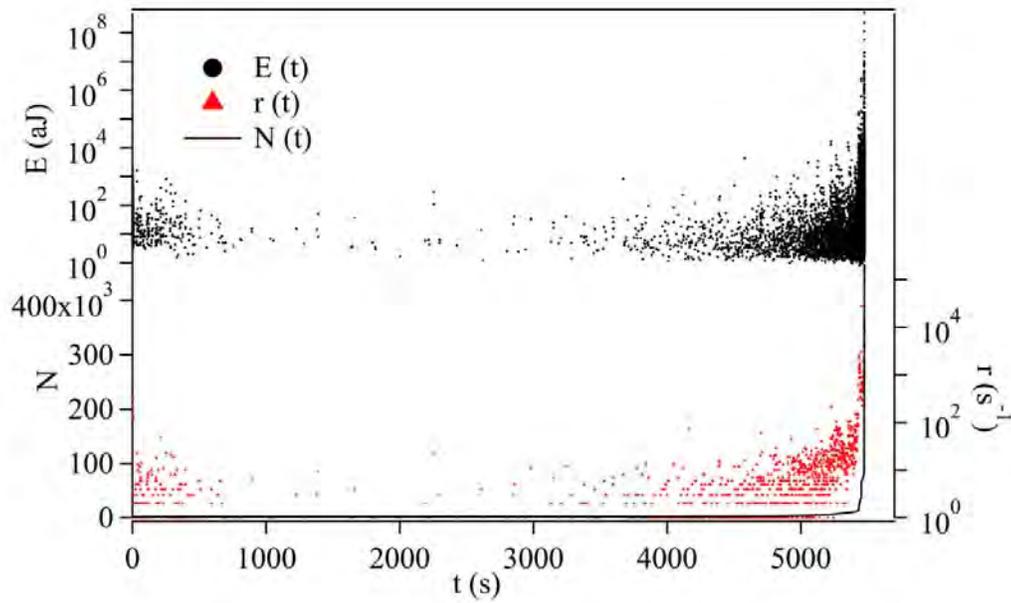
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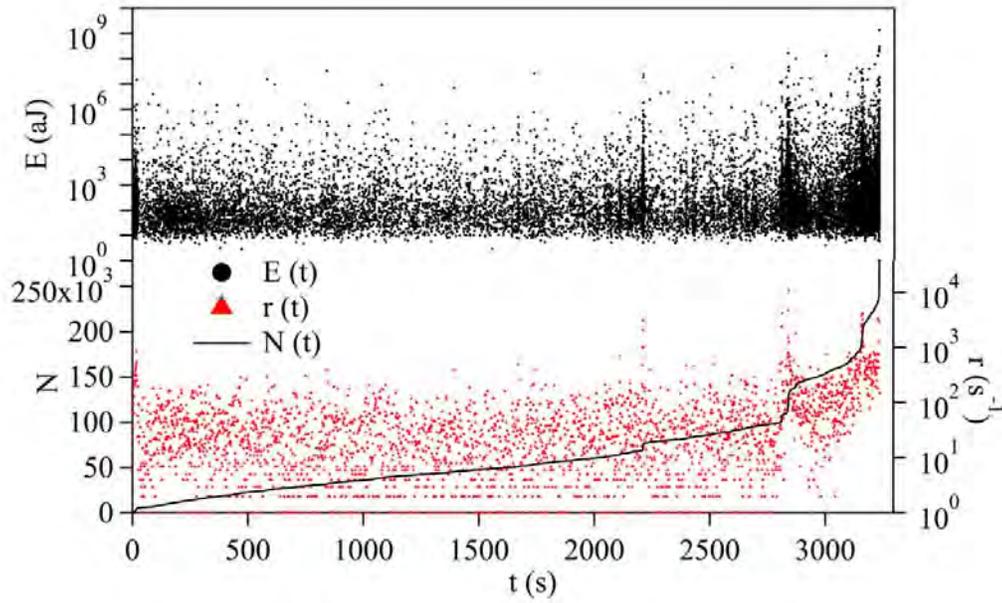
(a)



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(b)



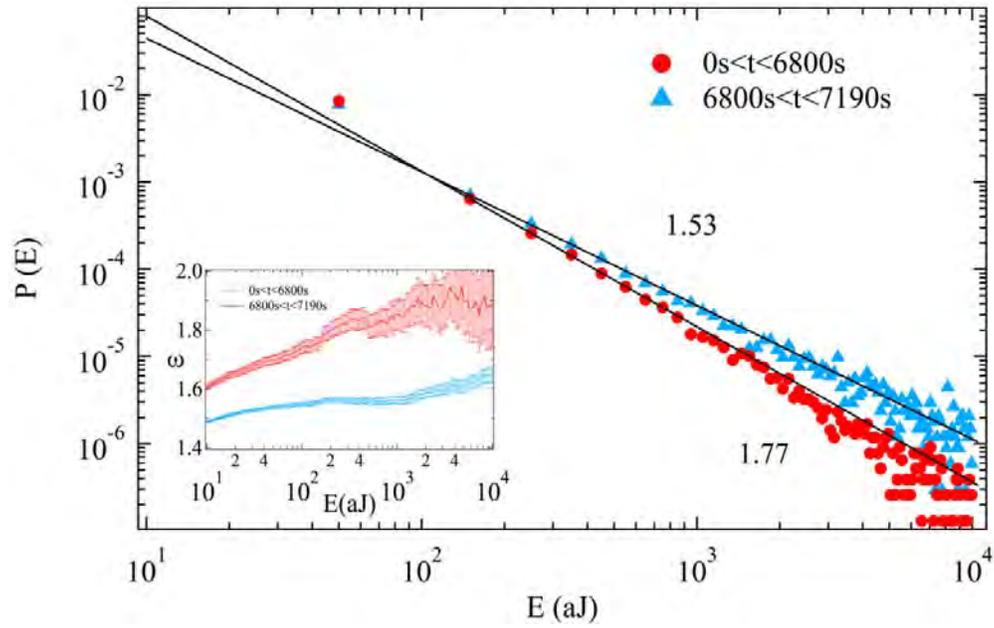
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(c)

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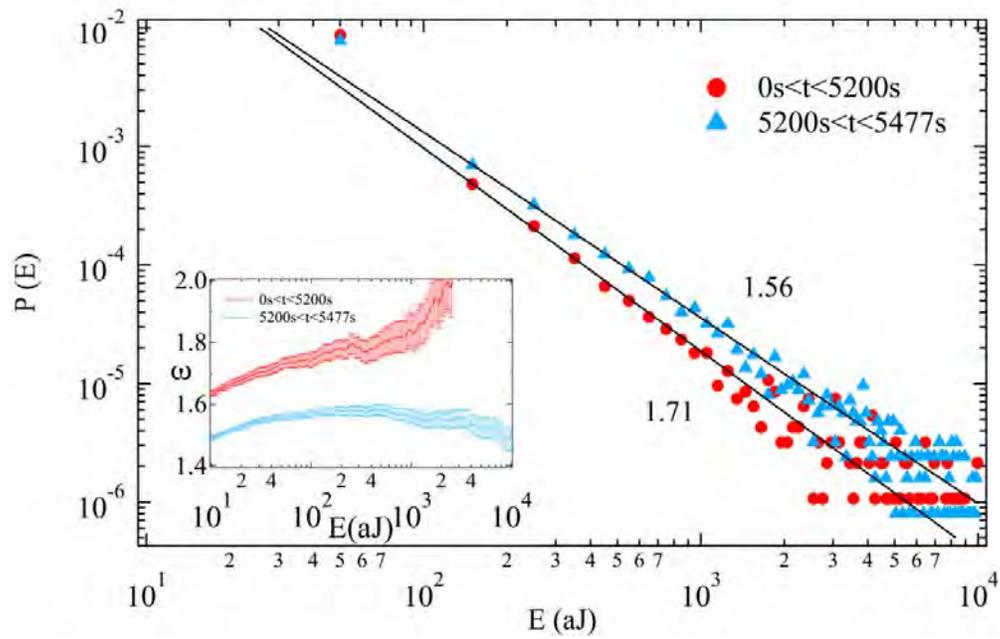
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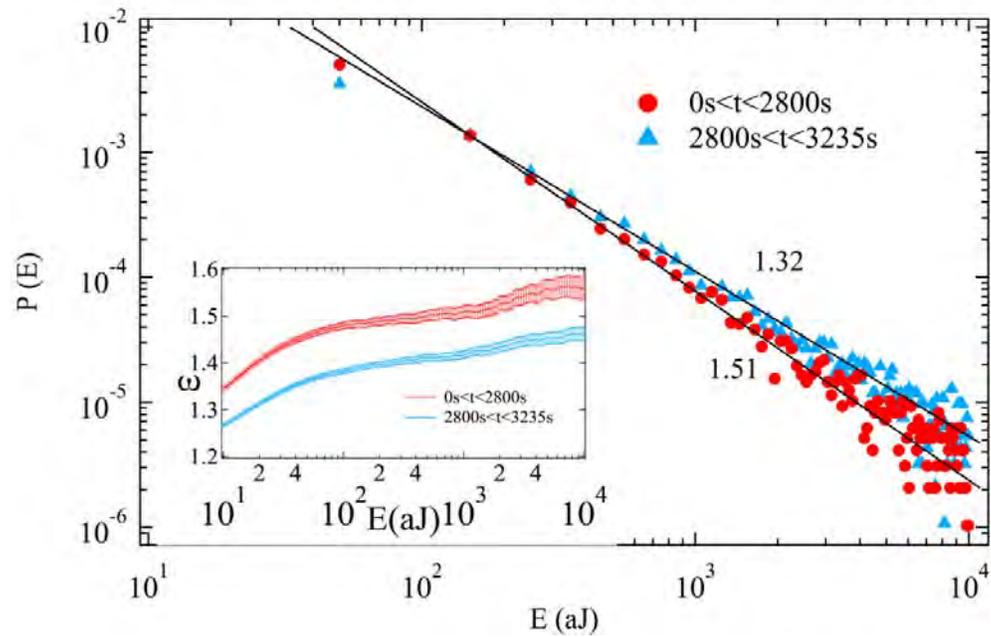
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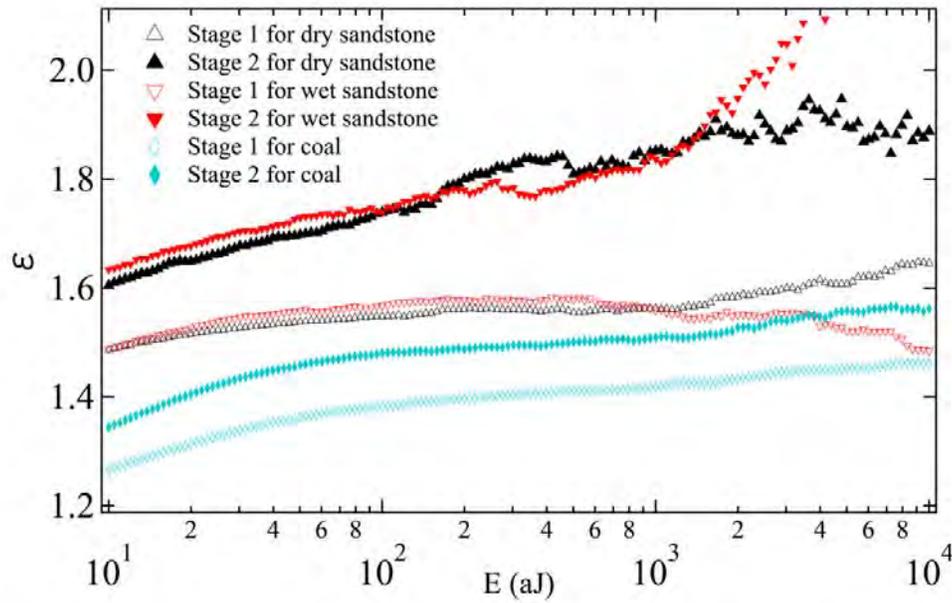
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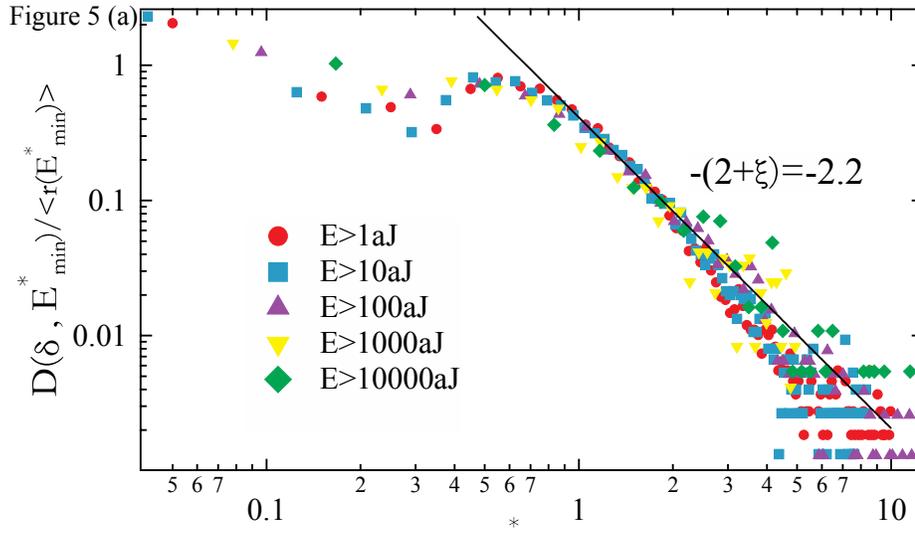
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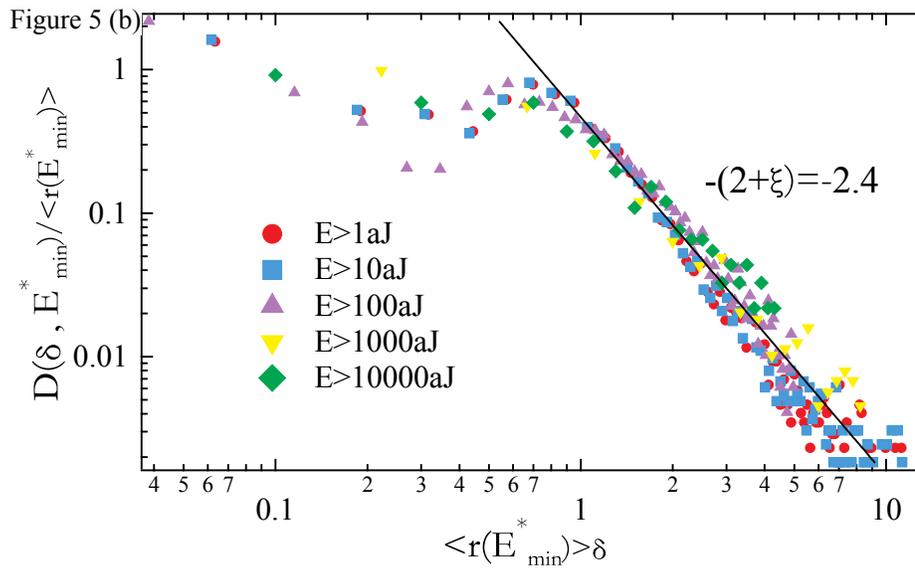
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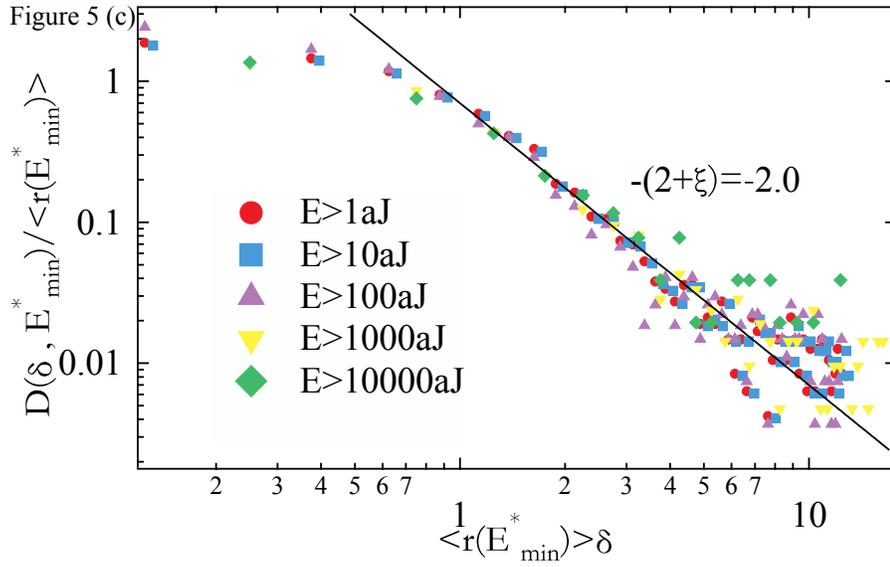
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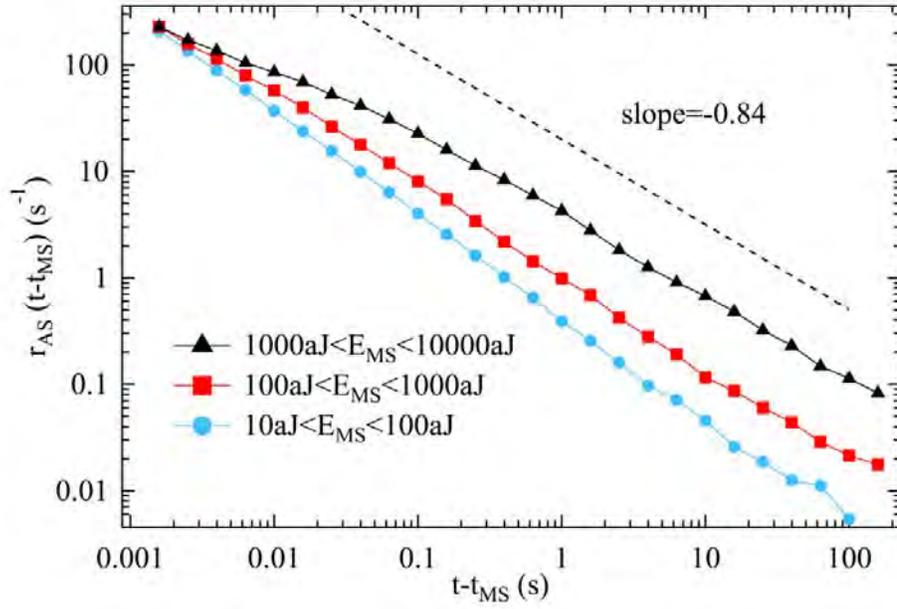
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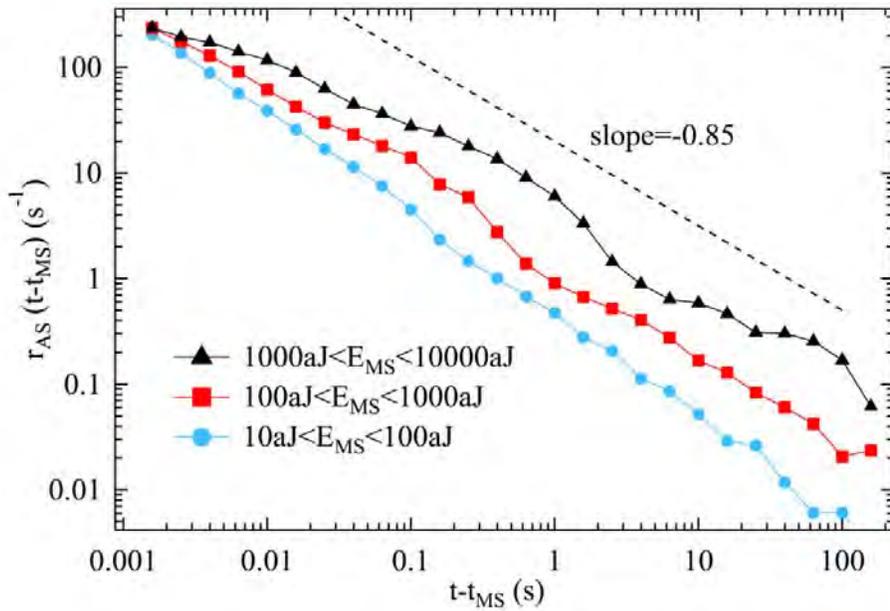
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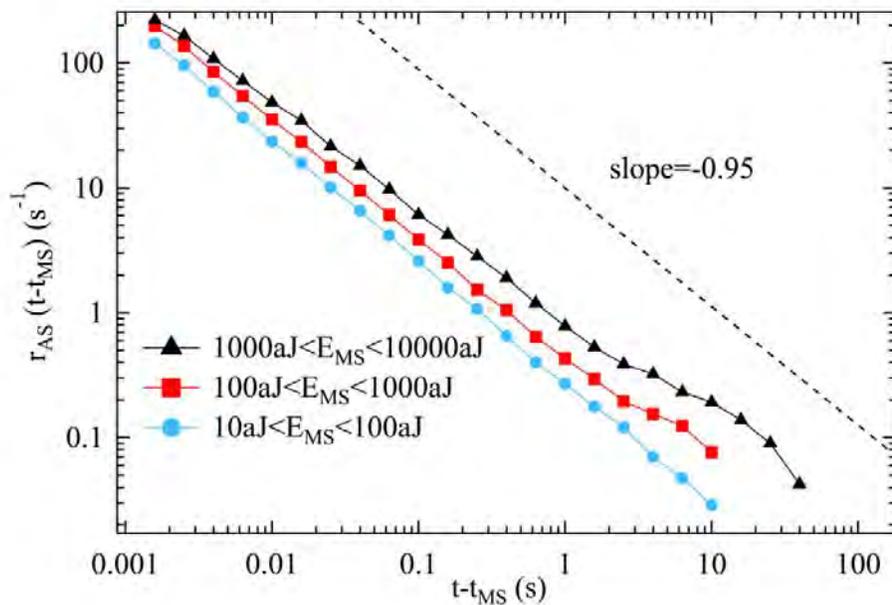
(a)



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(b)



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(c)

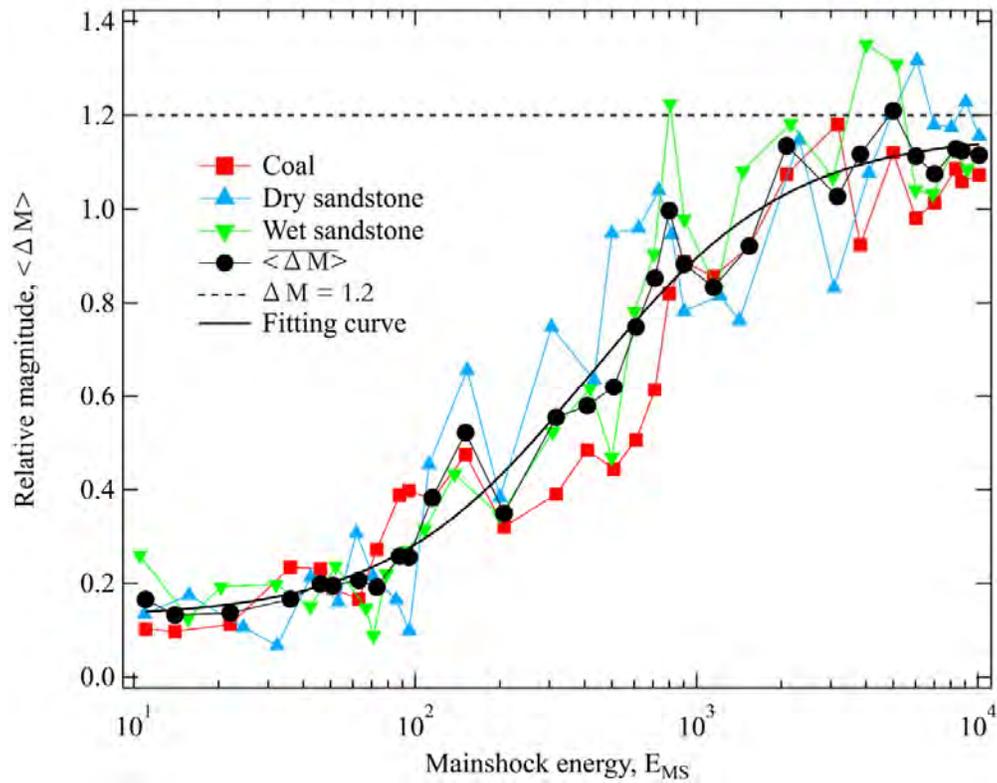
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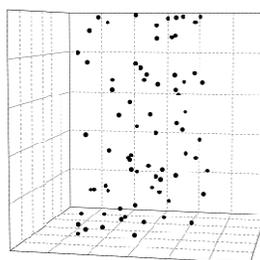
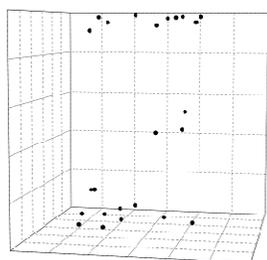
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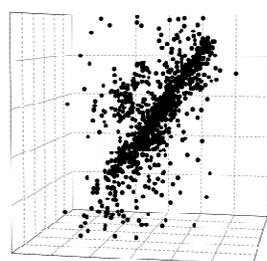


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(a)

(b)



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(c)

(d)

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