1	Revision 2
2	The crystal structure of turneaureite, Ca ₅ (AsO ₄) ₃ Cl, the
3	arsenate analogue of chlorapatite, and its relationships
4	with the arsenate apatites johnbaumite and svabite
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ABSTRACT

The crystal structure of turneaureite, ideally $Ca_5(AsO_4)_3Cl$, was studied using a specimen 20 from the Brattfors mine, Nordmark, Värmland, Sweden, by means of single-crystal X-ray 21 diffraction data. The structure was refined to $R_1 = 0.017$ on the basis of 716 unique reflections with 22 $F_0 > 4\sigma(F_0)$ in the $P6_3/m$ space group, with unit-cell parameters a = 9.9218(3), c = 6.8638(2) Å, V =23 585.16(4) $Å^3$. The chemical composition of the sample, determined by electron-microprobe 24 analysis, is (in wt% - average of 10 spot analyses): SO₃ 0.22, P₂O₅ 0.20, V₂O₅ 0.01, As₂O₅ 51.76, 25 SiO₂ 0.06, CaO 41.39, MnO 1.89, SrO 0.12, BaO 0.52, PbO 0.10, Na₂O 0.02, F 0.32, Cl 2.56, 26 H_2O_{calc} 0.58, O (= F+Cl) -0.71, total 99.04. On the basis of 13 anions per formula unit, the 27 28 empirical formula corresponds to $(Ca_{4,82}Mn_{0.17}Ba_{0.02}Sr_{0.01})_{\Sigma 5.02}(As_{2.94}P_{0.02}S_{0.02}Si_{0.01})_{\Sigma 2.99}O_{12}[Cl_{0.47}(OH)_{0.42}F_{0.11}]_{\Sigma 1.00}.$ 29

30 Turneaureite is topologically similar to the other members of the apatite supergroup: columns 31 of face-sharing M1 polyhedra running along c are connected through TO_4 tetrahedra with channels hosting M^2 cations and X anions. Owing to its particular chemical composition, the studied 32 turneaureite can be considered as a ternary calcium arsenate apatite; consequently it has several 33 partially-filled anion sites within the anion columns. Polarised single-crystal FTIR spectra of the 34 studied sample indicate stronger hydrogen bonding and less diverse short-range atom arrangements 35 around (OH) groups in turneaureite as compared to the related minerals johnbaumite and svabite. 36 An accurate knowledge of the atomic arrangement of this apatite-remediation mineral represents an 37 improvement in our understanding of minerals able to sequester and stabilize heavy metals such as 38 39 arsenic in polluted areas.

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Key-words: turneaureite, calcium arsenate, apatite supergroup, crystal structure, infrared
spectroscopy, Sweden.

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Introduction

Calcium arsenate apatites belong to the apatite supergroup, a series of minerals having the 45 general formula ${}^{IX}M1_2 {}^{VII}M2_3 ({}^{IV}TO_4)_3 X$ (Pasero et al. 2010). Three calcium arsenate members are 46 known: johnbaumite, svabite, and turneaureite, differing for the nature of the X anion, that is (OH), 47 F, and CI respectively. Whereas the crystal structures of johnbaumite and svabite were recently 48 investigated (Biagioni and Pasero 2013; Biagioni et al. 2016), the structural features of turneaureite 49 have not been described so far, even if the crystal structure of synthetic Ca₅(AsO₄)₃Cl was reported 50 by Wardojo and Wu (1996). In addition, natural specimens of turneaureite usually show a complex 51 anion composition, allowing a better understanding of the crystal chemistry of binary and ternary 52 53 calcium arsenate apatites. Indeed, whereas binary and ternary calcium phosphate apatites have been accurately studied (e.g., Hughes et al. 1989, 1990, 2014), few data are available for their arsenate 54 analogues. This paper aims at filling this gap. 55

Turneaureite was first described by Dunn et al. (1985) from three different localities, i.e. 56 Franklin, New Jersey, USA; Balmat, New York, USA; and Långban, Värmland, Sweden, as the 57 58 arsenate analogue of chlorapatite, Ca₅(PO₄)₃Cl, and the calcium analogue of mimetite, Pb₅(AsO₄)₃Cl. Only the specimen from the Swedish locality allowed the full-characterization of the 59 60 species and was designated as the holotype. Although the symmetry of apatites is typically hexagonal (space group $P6_3/m$), several phases have been reported with lower symmetry (e.g., 61 White et al. 2005; Baikie et al. 2007), sometimes showing superstructure reflections (e.g., 62 Chackmouradian and Medici 2005). This is particularly true for Cl-bearing apatites. As a matter of 63 fact neither deviation from the hexagonal symmetry nor any superstructure reflections in 64 turneaureite were reported by Dunn et al. (1985). The specimen from Långban has chemical 65 $(Ca_{4.85}Mn_{0.16}Pb_{0.02})_{\Sigma 5.03}[(AsO_4)_{2.42}(PO_4)_{0.54}]_{\Sigma 2.96}(Cl_{0.56}F_{0.39})_{\Sigma 0.95},$ with unit-cell 66 composition parameters a = 9.810(4), c = 6.868(4) Å, V = 572.4 Å³. The crystal structure of synthetic 67 $Ca_{5}(AsO_{4})_{3}Cl$ was refined by Wardojo and Hwu (1996) in the space group $P6_{3}/m$, with unit-cell 68

parameters a = 10.076(1), c = 6.807(1) Å, V = 598.4 Å³. Dai and Harlow (1991) presented, as a communication at a meeting, the results of the single-crystal X-ray diffraction study for the three natural calcium arsenate apatites, but to our knowledge the results of their work were never published.

Owing to the fact that an understanding of the crystal structure of As-rich minerals is useful in environmental remediation (e.g., Rakovan and Pasteris 2015), we carried out a combined chemical, structural, and spectroscopic study of turneaureite from Nordmark, Värmland, Sweden. The present data, in conjunction with data from johnbaumite and svabite (Biagioni and Pasero 2013; Biagioni et al. 2016), provide the basis for a comparative analysis of the crystal-chemical features of the three calcium arsenate minerals with the apatite structure.

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Experimental

81 The studied specimen (catalogue number NRM19532695) is from the Brattfors mine (latitude 59.83°N, longitude 14.12°E), Nordmark ore field, Filipstad, Värmland, Sweden. In this area there 82 are about twenty small mines and prospects, which have been worked mainly for magnetite ore 83 (e.g., Magnusson, 1929). The studied specimen of turneaureite consists of a fine-grained, irregularly 84 fine-banded, metamorphosed siliceous carbonate rock, mainly composed of Mn-bearing calcite. 85 Alleghanyite, jacobsite, and tephroite occurs as small (<0.5 mm) rounded grains together with 86 katoptrite and turneaureite in the calcite matrix. Grains of turneaureite (up to 3 mm) are rounded or 87 short prismatic to almost fibrous in habit, whereas katoptrite grains (up to 2 mm long) are typically 88 lath-shaped. Very rare rounded grains (< 1mm) of magnussonite are also observed. Dark red 89 aggregates of alleghanyite cover up to 1 cm^2 large areas in some micro-fissures. 90

Electron microprobe analyses were obtained by wavelength dispersive spectroscopy (WDS
mode) with a Cameca SX50 instrument at the "Istituto di Geologia Ambientale e Geoingegneria,

CNR" of Rome, Italy, using the following analytical conditions: accelerating voltage 15 kV, beam 93 current 15 nA, nominal beam diameter 1 µm. Counting time for one spot analysis was 20 s per 94 peak. Standards (element, emission line) are: baryte (BaLa, SKa), apatite (PKa), GaAs (AsLa), 95 wollastonite (CaK α , SiK α), vanadinite (VK α), rhodonite (MnK α), celestine (SrK α), galena (PbM α), 96 jadeite (NaK α), phlogopite (FK α), and sylvite (ClK α). The PAP routine was applied (Pouchou and 97 Pichoir 1991) for correction of recorded raw data. Ten spot analyses were performed; the studied 98 grain was found to be homogeneous. Chemical data are given in Table 1; the chemical formula, 99 based 13 anions formula unit, is 100 on per $(Ca_{4.82}Mn_{0.17}Ba_{0.02}Sr_{0.01})_{\Sigma 5.02}(As_{2.94}P_{0.02}S_{0.02}Si_{0.01})_{\Sigma 2.99}O_{12}[Cl_{0.47}(OH)_{0.42}F_{0.11}]_{\Sigma 1.00}$ 101

Polarised single-crystal infrared spectra of turneaureite were recorded with a Bruker Vertex 102 70 microscope spectrometer equipped with a halogen lamp source, a KBr beam-splitter, a 103 holographic ZnSe polarizer, and a midband MCT detector. The crystal was oriented by morphology 104 and optical microscopy and was doubly polished parallel to the a-c axis plane. The thickness of the 105 single crystal absorber was 38 μ m. Polarized absorption spectra were acquired parallel (E||E) and 106 perpendicular (E||O) to the c-axis over the wavenumber range 600–5000 cm⁻¹ with a resolution of 2 107 cm⁻¹ during 32 cycles. The spectral region of the O–H stretching bands of the recorded single-108 crystal spectra was fitted using the *PeakFit* 4.12 software (Jandel) assuming Gaussian peak shapes. 109

A crystal fragment $(230 \times 230 \times 100 \ \mu m \text{ in size})$ was selected for the single-crystal X-ray 110 diffraction study. Intensities were collected using a Bruker Smart Breeze diffractometer (50 kV, 30 111 112 mA) equipped with a CCD 4k low-noise area detector. Graphite-monochromatized MoK α radiation was used. The detector-to-crystal working distance was 50 mm. 558 frames were collected in ω and 113 114 φ scan modes in 0.5° slices; the exposure time was 10 s per frame. The data were integrated and 115 corrected for Lorentz and polarization, background effects, and absorption using the package of 116 softwares Apex2 (Bruker AXS Inc. 2004), resulting in a set of 753 independent reflections. The refinement of unit-cell parameters constrained to hexagonal symmetry gave a = 9.9218(3), c =117

118 6.8638(2) Å, V = 585.16(4) Å³. The statistical tests on the distribution of |E| values ($|E^2 - 1| =$ 119 1.019) and the systematic absences suggested the space group $P6_3/m$.

The crystal structure was refined starting from the atomic coordinates of chlorapatite (Hughes 120 et al. 1989) using Shelxl-2014 (Sheldrick 2015). Scattering curves for neutral atoms were taken 121 from the International Tables for Crystallography (Wilson 1992). The site occupation factors (s.o.f.) 122 of the three cation and four anion sites were initially refined using the following scattering curves: 123 124 Ca at the M1 and M2 sites; As at the T site; O at the O1, O2, O3 sites and Cl at the X site. Owing to the complex anion chemistry, the position of the latter site was found through difference-Fourier 125 map that showed the presence of a maximum at $(0, 0, \frac{1}{4})$. After a few cycles of isotropic 126 refinement, the R_1 converged to 0.079. In order to account for the occurrence of other elements 127 substituting for Ca, the s.o.f. of M1 and M2 were refined using the scattering curves of Ca vs Mn 128 129 and Ca vs Ba respectively. Only a minor improvement of the refinement was observed. After the introduction of the anisotropic displacement parameters for cations, the R_1 converged to 0.054. 130 Assuming an anisotropic model also for the O1, O2, and O3 positions, the R_1 value converged to 131 0.047. The displacement parameter of the X anion was refined isotropically. Indeed, the anisotropic 132 refinement of the displacement parameter of the X anion resulted in a very high U value [in 133 particular U^{33} , i.e. 0.262(6) Å²], suggesting the replacement of Cl by lighter atoms (in agreement 134 with chemical data) and the structural disorder affecting the column anions. Likely, these high 135 values of the anisotropic displacement parameters could mask the occurrence of several partially 136 occupied positions along the columns. Consequently, notwithstanding the good R value obtained 137 using an anisotropic description of the displacement parameter of the X position (i.e. $R_1 = 0.023$), an 138 isotropic model was preferred. In this way, a very high residual of 7.5 $e/Å^3$ at (0, 0, 0.33) was 139 found. By adding this additional position (named Xb), constraining the isotropic U value of Xa and 140 Xb to be equal, and freely refining their s.o.f., the R_1 converged to 0.018. The refined site scattering 141 142 indicated the occurrence of about 5.5 and 7.8 electrons per formula unit at Xa and Xb, respectively.

The Xb position was assumed to be occupied by Cl only, owing to the longer M2-Xb distance, 143 whereas Xa was assumed to have a mixed (OH, Cl, F) occupancy. The proposed site population, 144 taking into account the site multiplicity, was $(OH_{0.42}F_{0.11}Cl_{0.06})$ and $Cl_{0.41}$ at Xa and Xb, respectively. 145 The highest maximum residual was 1.14 $e/Å^3$ at (0, 0, 0.40); this position is similar to the split Cl 146 site found by Hughes et al. (1990) in ternary apatites. Consequently, we added this further position, 147 labeled as X_c, assuming for it a partial occupancy by Cl only, and removing the minor amount of 148 this element from the Xa site. The refinement converged to $R_1 = 0.0172$ for 716 unique reflections 149 with $F_{o} > 4 \sigma(F_{o})$ (0.0185 for all 753 reflections) and 42 refined parameters. The chemical formula 150 derived from the structure refinement (SREF) is $(Ca_{4,92}Ba_{0.05}Mn_{0.03})(AsO_4)_3[Cl_{0.47}(OH)_{0.42}F_{0.11}]$. 151 152 Details of data collection and refinement are given in Table 2. Fractional atom coordinates, site 153 occupancy factors, and isotropic or equivalent isotropic displacement parameters are reported in Table 3, whereas Table 4 gives anisotropic displacement parameters. Finally, Table 5 reports 154 selected bond distances, and Table 6 shows the bond-valence calculations obtained using the bond-155 valence parameters of Brese and O'Keeffe (1991). 156

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158 Crystal structure description

159 General features, cation coordination, and site population

The crystal structure of turneaureite is topologically similar to those of the other members of the apatite supergroup. It is composed by columns of face-sharing *M*1-centered polyhedra running along **c**; those polyhedra can be described as tricapped trigonal prisms. Adjacent columns are connected by TO_4 tetrahedra through corner-sharing. The *M*1 and *M*2 sites are Ca-dominant sites, with only a minor replacement by other cations, in agreement with chemical data. Refined site scattering at *M*1 (20.0 electrons) suggests only negligible replacement by heavier elements; consequently this site has a virtually pure Ca site population. The average <M1-O> distance is

2.579 Å, to be compared with 2.584 Å reported by Wardojo and Hwu (1996) for synthetic 167 Ca₅(AsO₄)₃Cl and 2.549 Å for chlorapatite studied by Hughes et al. (1989). Bond valence sum 168 (BVS) at M1, calculated using the proposed site population, is 1.98 valence units (v.u.). The M2 site 169 has a seven-fold coordination, with $\langle M2-\varphi \rangle = 2.529$ Å, compared with 2.505 and 2.493 Å for 170 synthetic $Ca_5(AsO_4)_3Cl$ and chlorapatite, respectively. The M2 site scattering (20.7 electrons) agrees 171 with the site population ($Ca_{0.93}Mn_{0.06}Ba_{0.01}$). The BVS at M2 is 2.00 v.u. The site population of the 172 M1+M2 sites, taking into account the site multiplicity, is consistent with (Ca_{4.79}Mn_{0.18}Ba_{0.03}), in 173 agreement with electron-microprobe data. Finally, the T site is occupied by As^{5+} , with minor 174 substitutions of P^{5+} , S^{6+} , and Si^{4+} . The average $\langle T-O \rangle$ distance is 1.678 Å, a little longer than the 175 176 bond distances observed in johnbaumite and svabite (1.671 and 1.674 Å, respectively; Biagioni and Pasero 2013; Biagioni et al. 2016) and close to that reported for synthetic Ca₅(AsO₄)₃Cl (1.682 Å) 177 by Wardojo and Hwu (1996) and for johnbaumite from Franklin (1.70 Å) by Henderson et al. 178 (2009). The BVS at T is 5.10 v.u.. 179

180 The anion columns

The studied specimen can be classified as turneaureite, because Cl is the dominant column anion. Actually, this sample could be defined as a ternary calcium arsenate apatite, with chemical composition Turn₄₇John₄₂Svab₁₁.

Three sites in the [001] columns were located, at coordinates $(0, 0, \frac{1}{4}), (0, 0, 0.31)$, and (0, 0, 0.31)184 0.37). Whereas in end-member (OH)-apatites, the hydroxyl group is displaced from the $(0, 0, \frac{1}{4})$ 185 position, being disordered 0.35 Å above or below the mirror plane (e.g., Hughes et al. 1989; 186 187 Biagioni and Pasero 2013), in turneaureite the (OH) groups have been located at the Xa position lying on the mirror plane. A minor substitution of (OH) by F is proposed. The Xb and Xc site have 188 been assumed to be occupied by Cl only. Actually, such split sites are inserted to model an electron 189 190 density that is continuously distributed along the anion column and around the mirror plane, 191 constrained by the necessity to avoid unrealistically short anion-anion distances.

In any column, there are five possible anion sites: i) Xa, located on the mirror plane, ii, iii) Xb, 192 located 0.38 Å above (hereafter Xb_a , where subscript a stands for above) and 0.38 Å below (Xb_b 193 where subscript b stands for below) the mirror plane, and iv, v) Xc, located 0.83 Å above (Xc_a) and 194 below (Xc_b) the mirror plane. Figure 1 show the anion-anion distances in the studied turneaureite. 195 Owing to the necessity to avoid short anion-anion contacts, only some configurations are possible, 196 confirming that complete disordering along anion columns is not realistic. Consequently, there 197 could be anion ordering within individual columns and disordering among the column themselves, 198 thus giving rise to completely disordered hexagonal structures (e.g., Hughes et al. 1989). 199

200 **Bond strain analysis**

201 Bosi (2014) demonstrated the occurrence of systematic errors in bond valence calculations 202 incident at the mixed occupancy sites. This type of error is very invidious because can give rise to a false indication of the presence of steric strain. However, as the systematic errors introduced into 203 the weighted BVS of turneaureite (Table 6) have been estimated to be small (< 0.05 v.u.), the 204 difference between BVS and expected weighted atomic valence can be interpreted in terms of bond 205 strain (Brown 2016). In detail, the anions at Xa may be considered as underbonded, because its BVS 206 is smaller than the expected value (0.33 v.u. and 0.53 v.u., respectively). On the other hand, Xb may 207 be considered as overbonded, because its BVS is larger than the expected value (0.75 v.u. and 0.41 208 v.u., respectively). Regarding the Xc site, its BVS agrees with the expected value (0.06 v.u.). The 209 above-mentioned deviations (bond strain) from the expected bond valence sum values are likely 210 related to the disorder in the actual position of the column anions and possibly to the unresolved 211 212 splitting of the M2 site.

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Discussion

215 Chlorine position in turneaureite

Hughes et al. (1989) determined the anion positions in end-member calcium phosphate 216 apatites and postulated that the anion positions in binary and ternary (F-OH-Cl) apatites would be 217 impossible to predict. Indeed, in agreement with these authors, an extensive rearrangement of the 218 end-member anion configurations may occur in ternary apatites in order to accommodate the large 219 Cl^{-} anion. In chlorapatite, Cl is located at (0, 0, 0.44), 1.2 Å above and below the mirror plane 220 located at (0, 0, 1/4) (Hughes et al. 1989); in synthetic Ca₅(AsO₄)₃Cl, Cl is at (0, 0, 0.37), 0.84 Å 221 above and below the mirror plane (Wardojo and Hwu 1996). In ternary phosphate apatites, a 0.4 Å 222 shift of the Cl⁻ anion toward the mirror plane was observed by Hughes et al. (1990). Such a shift is 223 224 accompanied by a splitting of the M2 position as a function of the neighboring anion to which M2-225 hosted cation is bonded. In some cases, the ordering of Cl and (OH) in anion columns could result 226 in a lowering of symmetry, from $P6_3/m$ to $P2_1/b$ with a doubling of the **b** axis (Chakhmouradian 227 and Medici 2006).

In the turneaureite studied, only the first phenomenon, i.e. the shift of Cl, occurs, whereas no hints of the occurrence of a doubling of the *b* parameter were observed. The splitting of the *M*2 site was not resolved, even if the U^{22} value is definitely larger than the corresponding value at *M*1 and those reported for *M*2 sites in johnbaumite and svabite (Biagioni and Pasero 2013; Biagioni et al. 2016), thus suggesting a possible positional disorder of this site in the {0001} plane.

In the studied sample, Cl is mainly located at (0, 0, 0.31), corresponding to a shift of 0.44 Å with respect to the Cl position in synthetic Ca₅(AsO₄)₃Cl. Another split position, having a low s.o.f., occurs at (0, 0, 0.37), corresponding to the coordinates of the Cl in the synthetic compound. This behavior is similar to that reported by Hughes et al. (1990) during their study of ternary apatites. Indeed they located Cl at (0, 0, 0.368), shifted 0.4 Å towards the mirror plane with respect to nearto-end-member chlorapatite; in addition, they found another split site, having a low site occupancy, at coordinates corresponding to that of Cl in chlorapatite, i.e. (0, 0, 0.44).

The Ca–Cl distances in turneaureite, i.e. 2.57 (M2-Xb) and 2.67 Å (M2-Xc), are similar to those given by Hughes et al. (1990) for ternary apatites, i.e. 2.63 and 2.70 Å for the two split *Ca*2 positions, in keeping with the chemical complexity of the turneaureite studied. These distances are definitely shorter than those reported for synthetic Ca₅(AsO₄)₃Cl and for chlorapatite, both showing Ca–Cl distances of ~2.76 Å (Hughes et al. 1989; Wardojo and Hwu 1996), in keeping with the shift of Cl toward the mirror plane in apatites having a complex anion chemistry and the unresolved splitting of the *M*2 site.

247 Comparison with johnbaumite and svabite

The refinement of the crystal structure of turneaureite, in conjunction with data from Biagioni and Pasero (2013) and Biagioni et al. (2016), completes the triptych of natural calcium arsenate apatites, allowing important comparison of their structural features.

Natural samples generally have non-ideal (non-end-member) compositions. Indeed, only the johnbaumite composition studied by Biagioni and Pasero (2013) was close to the ideal $Ca_5(AsO_4)_3(OH)$ formula, having only negligible amounts of Cl and with F being below the detection limit. The sample of svabite, on the contrary, contains significant amounts of (OH) replacing F. Concerning cation substitutions, Ca was replaced by Pb and Mn only in svabite and turneaureite, respectively. Phosphorus-to-arsenic substitution is trivial in all the studied samples (up to 0.04 apfu in johnbaumite).

Unit-cell parameters of johnbaumite and svabite are similar, with a = 9.72, c = 6.96 Å, V =570.4 Å³ for the former and a = 9.73, c = 6.98 Å, V = 572.1 Å³ for the latter. The unit-cell volume increase of svabite is only related to minor Pb replacing Ca. Indeed, the size of (OH)⁻ is slightly larger than F⁻ and consequently the unit-cell volume of johnbaumite should be larger than that of svabite. The unit-cell volume of turneaureite is significantly larger, i.e. 585.2 Å³ ($\Delta V = +2.3$ and +2.6% with respect to svabite and johnbaumite, respectively). Notably there is an expansion of the *a* parameter (a = 9.92 Å, $\Delta a \sim +2\%$) accompanied by a contraction of the *c* parameter (c = 6.86 Å,

 $\Delta c \sim -1.6\%$); this behavior is more evident in synthetic Ca₅(AsO₄)₃Cl, having a = 10.076 Å ($\Delta a \sim$ 265 +3.5%) and c = 6.807 ($\Delta c \sim -2.3\%$). This could accommodate an increase in the diameter of the 266 anion columns (Fig. 2), favoring the accommodation of the large Cl⁻ anion, as indicated by the 267 larger M2-M2 distance in turneaureite (4.40 Å) with respect to those observed in johnbaumite and 268 svabite (4.11-4.12 Å). Indeed, as the size of the X anion increases, the tunnels become wider 269 through reduction in the metaprism twist angle φ (e.g., White and Dong 2003; White et al. 2005), 270 defined as the angle O1-M1-O2 projected on (001) (White and Dong 2003; Lim et al. 2011). This 271 angle is used for the assessment of the distortion of the apatite structure from an ideal hexagonal 272 close packing of oxygen atoms. The metaprism twist angle in turneaureite, calculated according to 273 274 the formula proposed by Henderson et al. (2009), is 16.4°, definitely smaller than the corresponding 275 angles observed in johnbaumite (21.1°, Biagioni and Pasero 2013) and svabite (21.5°, Biagioni et 276 al. 2016), in agreement with the expansion of the anion columns in the (001) plane.

277 Fourier Transform Infrared Spectroscopy (FTIR) of turneaureite

The infrared spectra of turneaureite are very similar to those reported for svabite and 278 johnbaumite (Biagioni et al. 2016) and display strong absorption bands related to vibrational modes 279 in AsO₄-tetrahedra in the range 750-950 cm^{-1} and distinct absorption related to O–H stretching 280 modes in the range 3450-3600 cm⁻¹. As in spectra of the related minerals, the O–H stretching band 281 is polarized in E|| \mathbf{c} because of O-H dipole alignments along the crystallographic \mathbf{c} axis. The 282 recorded FTIR E||c| (E||E) spectrum of turneaureite in the O–H stretching region is compared with 283 those of svabite and johnbaumite in Figure 3. Whereas the positions of the O-H stretching bands 284 are almost identical in svabite and johnbaumite (Biagioni et al. 2016), they are shifted towards 285 lower wavenumbers by 5-15 cm⁻¹ in turneaureite, thus indicating stronger hydrogen bonding. In 286 addition, the intensity of the high-energy component of the O-H stretching region observed in 287 spectra of johnbaumite and svabite at ~3560 cm⁻¹ is strongly reduced in the turneaureite spectra. 288 289 This suggests less diverse short-range atom arrangements around the (OH) groups in turneaureite

compared to the two related minerals. Using the IR method for determining the (OH) concentration
in apatite (Wang et al. 2011), the H₂O content in the turneaureite specimen should be close to 0.28
wt%, which is lower than the 0.58 wt% calculated for the empirical formula on the basis of
electron-microprobe analysis. As in svabite and johnbaumite (Biagioni et al. 2016), the calculated
H₂O concentration is approximately one half of that estimated from chemical data.

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Implications

The refinement of the crystal structure of turneaureite through single-crystal X-ray diffraction using a natural specimen from Sweden has a two-fold relevance, i) adding new data to the knowledge of the crystal chemistry of calcium arsenate apatites, and ii) giving further insights into the complex anion arrangement in anion columns owing to its complex chemistry.

The occurrence of arsenic in surface and groundwaters in several localities world-wide (e.g., 301 302 in south-eastern Asia; Charlet and Polya 2006) and its observed adverse health effects emphasize 303 the importance of calcium arsenate apatites, owing to their potential role as sequestrators and stabilizers of arsenic from polluted water (e.g., Magalhães and Williams 2007; Liu et al. 2014). In 304 order to explore their possible application in environmental remediation (e.g., Rakovan and Pasteris 305 2015), a deep knowledge of their crystal chemistry is mandatory, because the atomic arrangement 306 of their crystal structure strongly affects their physical properties. Although several high-quality 307 crystal structure refinements are available for calcium phosphate apatites (e.g., White et al. 2005), 308 only a few investigations through single-crystal X-ray diffraction have been reported so far for the 309 310 corresponding arsenate analogs. Recently, Biagioni and Pasero (2013) and Biagioni et al. (2016) gave the first structural data obtained through single-crystal techniques on natural samples of 311 312 $Ca_5(AsO_4)_3OH$ (johnbaumite) and $Ca_5(AsO_4)_3F$ (svabite). As stated above, the refinement of the crystal structure of turneaureite completes the triptych of natural calcium arsenate apatites, 313 improving the knowledge of the crystal chemistry of this group. 314

In addition, the complex anion chemistry of the turneaureite studied in this work, showing the 315 simultaneous presence of Cl, (OH), and minor F as column anions, is particularly intriguing. 316 Indeed, apatites are among the few minerals showing anion substitution series. Owing to the 317 different sizes of the three column anions F, (OH), and Cl, as well as to the steric interactions 318 among those anions in the anion columns, particularly complex atomic arrangements could result. 319 As stressed by Hughes et al. (2014), despite the widespread interest in apatites and the dependence 320 of all their properties on the atomic arrangements, the crystal structures of binary and ternary 321 apatites are not well understood as the anion distribution is not predictable from the structures of 322 end-members. Consequently, several studies have been focused on the atomic arrangements in the 323 324 anion columns (e.g., Hughes 2015). With respect to synthetic Ca₅(AsO₄)₃Cl (Wardojo and Hwu 325 1996), where only Cl was present, the studied turneaureite represents a ternary arsenate apatite that 326 offers the possibility to describe the anion substitution series between turneaureite itself and the two other arsenate apatites (johnbaumite and svabite). The results show a Cl shifting toward the mirror 327 planes, similar to that reported in ternary calcium phosphate apatites (Hughes et al. 1990). 328

As the understanding of these anion substitutions is more than an academic exercise (Hughes and Rakovan 2015), being essential to take into account several scientific aspects (e.g., the volatile behavior and budgets in melts and related fluids) as well as technological properties of apatites, the present study represents a further step in the knowledge of the atomic arrangements and chemical substitution mechanisms of this important supergroup of minerals.

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418 **Table captions**

- **Table 1** Electron-microprobe data (mean of 10 spot analyses, in wt%) of turneaureite, estimated
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- 421 calculated with the assumption (Cl+F+OH) = 1 apfu.
- 422 Table 2 Crystal data and summary of parameters describing data collection and refinement for
- 423 turneaureite.
- 424 Table 3 Site occupancy factors (s.o.f.), fractional atom coordinates, and isotropic (*) or
- 425 equivalent isotropic displacement parameters (in Å²) for turneaureite. U_{eq} is defined as one third of
- 426 the trace of the orthogonalized U^{ij} tensor.
- 427 **Table 4** Anisotropic displacement parameters (in $Å^2$) for turneaureite.
- 428 **Table 5** Selected bond distances (in Å) for turneaureite.
- **Table 6** Weighted bond valences for turneaureite, in valence units (v.u.).
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431 **Figure captions**

- 432 Fig. 1 Anion-anion distances (in Å) for column anions. Same labels as in the text. Grey cells
- 433 indicate configurations not allowed owing to too short interionic distances.
- **Fig. 2** Comparison among the anion colums in johnbaumite (a), svabite (b), and turneaureite (c).
- 435 The M2-M2 distances are shown. Atoms are drawn as thermal ellipsoids. Symbols: black = M2 site;
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- 438 Fig. 3 Infrared $E \parallel E (E \parallel c)$ spectra of turneaureite (thick line) in the O-H stretching region
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- 442 **Table 1** Electron-microprobe data (mean of 10 spot analyses, in wt%) of turneaureite, estimated
- standard deviation (e.s.d.), and atoms per formula unit (apfu), on the basis of 13 anions. H_2O was

Oxide	wt%	range	e.s.d.	apfu
SO ₃	0.22	0.02 - 1.10	0.31	0.018
P_2O_5	0.20	0.12 – 0.26	0.08	0.018
V_2O_5	0.01	0.00 - 0.06	0.02	0.001
As_2O_5	51.76	50.27 – 52.40	0.78	2.942
SiO ₂	0.06	0.03 - 0.09	0.02	0.007
CaO	41.39	40.45 – 41.89	0.63	4.821
MnO	1.89	1.54 – 3.37	0.65	0.174
SrO	0.12	0.05 - 0.28	0.08	0.008
BaO	0.52	0.11 – 2.38	0.82	0.022
PbO	0.10	0.00 - 0.24	0.08	0.003
Na ₂ O	0.02	0.00 - 0.06	0.02	0.004
F	0.32	0.11 – 0.56	0.14	0.110
CI	2.56	2.15 – 2.84	0.21	0.472
$H_2O_{(calc)}$	0.58			0.421
O = F + Cl	-0.71			
Total	99.04			

444 calculated with the assumption (Cl+F+OH) = 1 apfu.

Table 2 – Crystal data and summary of parameters describing data collection and refinement for

447 turneaureite.

Crystal data								
Crystal size (mm)	0.23 x 0.23 x 0.10							
Cell setting, space group	Hexagonal, <i>P</i> 6 ₃ / <i>m</i>							
a, c (Å)	9.9218(3), 6.8638(2)							
$V(Å^3)$	585.16(4)							
Z	2							
Data collection and	refinement							
Radiation, wavelength (Å)	Mo <i>K</i> α, 0.71073							
Temperature (K)	298							
Detector-to-sample distance (mm)	50							
Number of frames	558							
Rotation width per frame (°)	0.5							
Maximum observed 20 (°)	65.05							
Measured reflections	2720							
Unique reflections	753							
Reflections with $F_{o} > 4\sigma(F_{o})$	716							
R _{int} after absorption correction	0.0156							
R_{σ}	0.0146							
	-8 ≤ <i>h</i> ≤ 13							
Range of <i>h</i> , <i>k</i> , <i>l</i>	-15 ≤ <i>k</i> ≤ 10							
	-10 ≤ <i>l</i> ≤ 5							
$R_1 [F_0 > 4 \sigma(F_0)]$	0.0172							
R_1 (all data)	0.0185							
wR_2 (on F_0^2)	0.0447							
Goof	1.108							
Number of I.s. parameters	42							
Maximum and minimum residual	0.75 (at 0.56 Å from <i>M</i> 2) -0.88 (at 0.74 Å from <i>M</i> 2)							

- 451 **Table 3** Site occupancy factors (s.o.f.), fractional atom coordinates, and isotropic (*) or
- 452 equivalent isotropic displacement parameters (in Å²) for turneaureite. U_{eq} is defined as one
 - Wyckoff Site y/b s.o.f. x/a z/c $U_{\rm eq/iso}$ position 0.01344(14) *M*1 2/3 1/3 0.00395(8) 4f $Ca_{0.328(3)}Mn_{0.005(3)}$ 0.02306(18) М2 6h Ca_{0.491(1)}Ba_{0.009(1)} 0.01102(6) 0.26117(7) 1⁄4 Т 6h As_{0.50} 0.37437(3) 0.40457(3) 1⁄4 0.01006(8) 01 0.3416(2) 1⁄4 0.0198(4) 6h O_{0.50} 0.5020(2) 02 0.6012(2) 1⁄4 0.0171(3) 6h O_{0.50} 0.4663(2) O3 12*i* O_{1.00} 0.25644(16) 0.34708(18) 0.44470(19) 0.0217(3) (OH)_{0.070}F_{0.018} 0 0 Xa 2a 1⁄4 0.0160(5)*

0

0

0

0

0.3055(6)

0.370(4)

0.0160(5)*

0.0160(5)*

453 third of the trace of the orthogonalized U^{ij} tensor.

45	54
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Хb

Хc

4e

4e

455

456 **Table 4** – Anisotropic displacement parameters (in $Å^2$) for turneaureite.

 $\text{Cl}_{0.068}$

 $CI_{0.010}$

Site	U^{11}	U^{22}	U ³³	U^{23}	U ¹³	U^{12}
<i>M</i> 1	0.01587(18)	0.01587(18)	0.0086(2)	0	0	0.00794(9)
М2	0.0162(2)	0.0346(3)	0.0117(2)	0	0	0.0077(2)
Т	0.01083(11)	0.01054(11)	0.01045(11)	0	0	0.00658(8)
01	0.0230(9)	0.0338(10)	0.0146(7)	0	0	0.0233(9)
02	0.0178(8)	0.0098(7)	0.0225(8)	0	0	0.0060(6)
O3	0.0188(6)	0.0351(7)	0.0156(6)	0.0097(6)	0.0066(5)	0.0168(6)

458 **Table 5** – Selected bond distances (in Å) for turneaureite.

<i>M</i> 1	O1 (× 3)	2.3800(13)	М2	O3 (× 2)	2.3159(13)	Т	01	1.6681(18)
	O2 (× 3)	2.4609(14)		02	2.345(2)		O3 (× 2)	1.6772(13)
	O3 (× 3)	2.8953(16)		O3 (× 2)	2.5232(15)		02	1.6909(17)
				Xa	2.5384(7)			
				Xb	2.5669(9)			
				Xc	2.669(9)			
				O1	3.121(2)			
	< <i>M</i> 1–O>	2.579		< <i>M</i> 2–O>	2.529		< <i>T</i> _O>	1.678

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459

462 **Table 6** – Weighted bond valences for turneaureite, in valence units (v.u.).

Site	01	02	O3	Xa	Xb	Xc	Σ cations	
<i>M</i> 1	^{3x→} 0.32 ^{×2↓}	^{3x→} 0.26 ^{×2↓}	^{3x→} 0.08		0.25 ^{×3↓} 0			1.98
140	0.04	0.36	^{2x→} 0.39	0.11 ^{×3↓}		0.02 ^{x3↓}	2.00	
IVIZ			^{2x→} 0.22				2.00	
Т	1.31	1.23	^{2x→} 1.28				5.10	
Σ anions	1.99	2.11	1.97	0.33	0.75	0.06		

Note: left and right superscripts indicates the number of equivalent bonds involving cations and anions, respectively. For sites with mixed occupancy, the bond valences have been weighted according to the proposed site population: $M1 = Ca_{1.00}$; $M2 = Ca_{0.93}Mn_{0.06}Ba_{0.01}$.

463

464

- 466 Fig. 1 Anion-anion distances (in Å) for column anions. Same labels as in the text. Grey cells
- 467 indicate configurations not allowed owing to too short interionic distances.

			at z -	- %4		
Φ		Ха	Xb _a	Xb_b	Xc _a	Xc _b
or plan	Xa	3.43	3.81	3.05	4.26	2.61
th mirr	Xb _a	3.05	3.43	2.67	3. <mark>8</mark> 8	2.23
ated wi at $z = \frac{1}{2}$	Xb_b	3.81	4.19	3.43	4.64	2.99
associ	Xc _a	2.61	2.99	2.23	3.43	1.78
Anion	Xc_b	4.26	4.64	3.88	5.08	3.43

Anion associated with mirror plane at $z = \frac{3}{4}$

468

- 470 Fig. 2 Comparison among the anion colums in johnbaumite (a), svabite (b), and turneaureite (c).
- 471 The M2-M2 distances are shown. Atoms are drawn as thermal ellipsoids. Symbols: black = M2 site;
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- 473 dominant sites.



475

Fig. 3 – Infrared E||E|(E||c) spectra of turneaureite (thick line) in the O–H stretching region compared with those of johnbaumite (thin broken line) and svabite (thin dotted line) (Biagioni et al. 2016).



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Anion associated with mirror plane at $z = \frac{3}{4}$

	Xa	Xb _a	Xb _b	Xc _a	Xc _b
Xa	3.43	3.81	3.05	4.26	2.61
Xb _a	3.05	3.43	2.67	3.88	2.23
Xb _b	3.81	4.19	3.43	4.64	2.99
Xc _a	2.61	2.99	2.23	3.43	1.78
Xc _b	4.26	4.64	3. <mark>88</mark>	5.08	3.43



