Revision 1

Pyradoketosite, a new, unexpected, polymorph of Ag₃SbS₃ from the Monte Arsiccio mine (Apuan Alps, Tuscany, Italy)

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ABSTRACT

Although everything seemed clear about the Ag–Sb–S compounds belonging to one of the more deeply studied experimental systems, nature allowed us to discover a new polymorph of Ag$_3$SbS$_3$, which could represent a compound for assessing new technological potentialities. The new mineral species pyradoketosite, Ag$_3$SbS$_3$ (IMA 2019-132), was discovered in the pyrite + baryte + iron oxide ore deposit of the Monte Arsiccio mine, Apuan Alps, Tuscany, Italy. It occurs as brittle orange acicular crystals, up to 200 μm in length and 25 μm in thickness, with adamantine luster. Under reflected light, pyradoketosite is slightly bluish grey, with abundant orange internal reflections. Bireflectance is weak and anisotropism was not observed, being masked by abundant internal reflections. Minimum and maximum reflectance data for the wavelengths recommended by the Commission on Ore Mineralogy [$R_{\text{min}}/R_{\text{max}}$ (%), (λ, nm)] are: 32.8/32.9 (470), 30.2/30.7 (546), 29.0/29.6 (589), and 27.5/28.4 (650). Electron microprobe analysis gave (mean of 6 spot analyses, in wt%): Ag 59.81, Sb 22.63, S 17.78, total 100.22. On the basis of (Ag+Sb) = 4 atoms per formula unit, the empirical formula of pyradoketosite is Ag$_{2.996(11)}$Sb$_{1.004(11)}$S$_{2.996(15)}$. Pyradoketosite is monoclinic, space group $P2_1/n$, with $a = 13.7510(15)$, $b = 6.9350(6)$, $c = 19.555(2)$ Å, $\beta = 94.807(4)^\circ$, $V = 1858.3(3)$ Å$^3$, $Z = 12$. The crystal structure was solved and refined to $R_1 = 0.063$ on the basis of 2682 unique reflections with $F_o > 4\sigma(F_o)$ and 191 refined parameters. The crystal structure of pyradoketosite can be described as formed by the alternation of {101} layers: an Sb-rich layer, Sb$_3$AgS$_3$, and two distinct Ag$_8$S$_6$ layers. This layered organization allows to identify structural relationships with the wittichenite-skinnerite pair. Pyradoketosite is associated with pyrargyrite, tetrahedrite-(Hg), valentinite, and probable pyrostilpnite in baryte + dolomite + quartz veins embedded in metadolostone. Its name derives from the old Greek words “πυρ” (fire) and “ἀδόκητος” (unforeseen), owing to the unexpected occurrence of this third polymorph of the compound Ag$_3$SbS$_3$. 

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INTRODUCTION

More than 150 Ag-chalcogenides are currently known as valid mineral species, mainly represented by sulfosalts (e.g., Moëlo et al. 2008; Bindi and Biagioni 2018). Indeed, silver is a chemical constituent of several minerals belonging to important groups of sulfosalts, e.g., sartorite (Makovicky and Topa 2015), lillianite (e.g., Makovicky and Topa 2014), polybasite (e.g., Bindi et al. 2007, 2020), and tetrahedrite (Biagioni et al. 2020b) groups. Despite the wide number of mineral species, the Ag–Sb–S system currently has only six approved sulfosalts, i.e., baumstarkite, cuboarpygrite, miargyrite, pyrargyrite, pyrostilpnite, and stephanite. Baumstarkite (triclinic), cuboarpygrite (cubic), and miargyrite (monoclinic) can be considered as polymorphs of the compound AgSbS$_2$ (Smith et al. 1997; Walenta 1998; Effenberger et al. 2002), although Kitakaze et al. (2006) questioned the dimorphic relations between baumstarkite and miargyrite. Trigonal pyrargyrite and monoclinic pyrostilpnite are the two known dimorphs of Ag$_3$SbS$_3$ (Laufek et al. 2010; Biagioni et al. 2020c), with the latter being the low-$T$ polymorph (e.g., Chang 1963; Keighin and Honea 1969). Stephanite, Ag$_3$SbS$_4$, is another low-$T$ Ag-sulfosalt, stable below 197 ± 5°C (e.g., Keighin and Honea 1969), with orthorhombic symmetry (Leitl et al. 2009).

During the study of the sulfosalt assemblages of the Monte Arsiccio mine (Apuan Alps, northern Tuscany, Italy), two samples showing μm-sized acicular crystals, orange in color, were observed. Electron microprobe and single-crystal X-ray diffraction studies showed it to be a new polymorph of Ag$_3$SbS$_3$. The mineral and its name were approved by the Commission on New Minerals, Nomenclature and Classification of the International Mineralogical Association (CNMNC-IMA) under the number IMA 2019-132. Holotype material is deposited in the mineralogical collection of the Museo di Storia Naturale, Università di Pisa, Via Roma 79, Calci, Pisa (Italy), under catalogue number 19913. The name pyradoketosite alludes to the unforeseeable nature of this mineral and it is formed from the old Greek words “πυρ” (fire) and “άδόκητος”
(unforeseen); the name also reflects the surprise at finding a new polymorph of the “ruby silvers” Ag$_3$SbS$_3$, as both the dimorphs pyrargyrite and pyrostilpnite have been known for a long time.

This paper describes this new silver sulfosalt and discusses its relationships with the other known “ruby silvers” as well as with the members of the wittichenite-skinnerite group having structural similarities with pyradoketosite.

**OCCURRENCE AND MINERAL DESCRIPTION**

Pyradoketosite is very rare and was identified in only two specimens from the Sant’Olga level, Monte Arsiccio mine (latitude 43°58’N, longitude 10°17’E), Apuan Alps, northern Tuscany, Italy. This mine exploited, up to the end of the 1980s, a pyrite + baryte + iron oxide (magnetite, hematite, “limonite”) ore deposit located close to the contact between a Paleozoic metasedimentary-metavolcanic sequence and Triassic metadolostone, in the north-eastern sector of the Sant’Anna tectonic window. The Monte Arsiccio mine is the type locality for nine other mineral species, among which are some other sulfosalts: boscardinite (Orlandi et al. 2012), protochabournéite (Orlandi et al. 2013), arsiccioite (Biagioni et al. 2014), and andreadiniite (Biagioni et al. 2018). Pyradoketosite is the tenth new mineral discovered at this locality. A review of the geological setting of this mine is given in Biagioni et al. (2020a) and references therein.

Pyradoketosite occurs as acicular crystals, striated parallel to the elongation, up to 200 μm in length and 25 μm in thickness (Figure 1). Color and streak are orange. The mineral is translucent, with an adamantine luster. Owing to the small size and extreme rarity of pyradoketosite, hardness was not measured. This mineral is brittle. No cleavage was observed. Density was not measured; on the basis of the empirical formula and unit-cell parameters refined from single-crystal X-ray diffraction data, the calculated density is 5.809 g/cm$^3$.

Under reflected light, pyradoketosite is slightly bluish grey in color, with abundant orange internal reflections. Pleochroism was not observed. Bireflectance is weak and anisotropism was not
observed, being masked by abundant internal reflections. Pyradoketosite is weakly light sensitive.

Reflectance values (SiC as standard) were measured in air (Natural History Museum, London) and are reported in Table 1 and shown in Figure 2.

Pyradoketosite occurs in baryte + dolomite + quartz veins, in association with valentinite, a tetrahedrite-group mineral [likely tetrahedrite-(Hg), on the basis of energy dispersive spectrometry (EDS) data collected on an unpolished grain], and some unidentified phases. In one sample, pyradoketosite occurs in a dissolution cavity of a previous unknown sulfosalt, along with valentinite. Figure 1 shows the close association of the acicular crystal of pyradoketosite with two other phases. Both have the same chemical composition as pyradoketosite. One of them, forming equant crystals, with a trigonal symmetry, was identified as pyrargyrite, on the basis of single-crystal X-ray diffraction data, whereas the other, characterized by a tabular habit, is tentatively attributed to pyrostilpnite on the basis of crystal morphology.

CHEMICAL DATA

Preliminary chemical analyses of pyradoketosite performed through EDS showed Ag, Sb and S as the only elements with $Z > 8$. Quantitative data were obtained through wavelength dispersive spectrometry (WDS mode) with a Superprobe JEOL JXA8200 electron microprobes at the “Eugen F. Stumpfl laboratory”, Leoben University, Austria, using the following analytical conditions: accelerating voltage 20 kV, beam current 10 nA, nominal beam diameter 1 μm. The peak and backgrounds counting times were 15 and 5 seconds, respectively. The following standards (element, emission line) were used: electrum Ag$_{70}$Au$_{30}$ (Ag$L\alpha$) and stibnite (S$K\alpha$, Sb$L\alpha$). Chemical data are given in Table 2. The empirical formula, based on 4 (Ag + Sb) atoms per formula unit (apfu), is Ag$_{2.996(11)}$Sb$_{1.004(11)}$S$_{2.996(15)}$. The ideal formula of pyradoketosite, Ag$_3$SbS$_3$, corresponds to (in wt%):

Ag 59.76, Sb 22.48, S 17.76, total 100.00.
X-RAY CRYSTALLOGRAPHY AND STRUCTURE REFINEMENT

The X-ray powder diffraction pattern of pyradoketosite was collected using a 114.6 mm diameter Gandolfi camera and Ni-filtered CuKα radiation. Owing to the very small size of the available material, the observed pattern showed only few and weak diffraction lines despite the long exposure time (one week). Table 3 reports the observed X-ray powder diffraction pattern along with that calculated on the basis of the structural model described below.

Single-crystal X-ray diffraction data were collected using a Bruker Smart Breeze three-circle diffractometer equipped with an air-cooled Photon II CCD detector, with graphite-monochromatized MoKα radiation (Dipartimento di Scienze della Terra, Università di Pisa). The detector-to-crystal distance was set at 50 mm. A total of 1072 frames were collected in ω scan mode in 0.5° slices, with an exposure time of 25 s per frame. Intensity data were corrected for Lorentz-polarization factors, absorption and background using the package of software Apex3 (Bruker AXS Inc. 2016).

Pyradoketosite is monoclinic, with unit-cell parameters \(a = 13.7510(15)\), \(b = 6.9350(6)\), \(c = 19.555(2)\) Å, \(β = 94.807(4)^°\), \(V = 1858.3(3)\) Å\(^3\). The \(a:b:c\) ratio is 1.9828:1:2.8198. The analysis of the reflection conditions led unequivocally to the choice of the space group \(P2_1/n\). This cell can be transformed in the standard space group \(P2_1/c\) through the matrix \(R = [1\ 0\ 0\ |\ 0\ -1\ 0\ |\ -1\ 0\ -1]\), resulting in the unit-cell parameters \(a = 13.7510(15)\), \(b = 6.9350(6)\), \(c = 22.944(2)\) Å, \(β = 121.864(5)^°\), \(V = 1858.3(3)\) Å\(^3\). However, the more orthogonal \(P2_1/n\) space group was preferred, and the crystal structure was solved in this space group through direct methods using Shelxs-97 and refined using Shelxl-2018 (Sheldrick 2015). Neutral scattering curves for Ag, Sb, and S were taken from the International Tables for Crystallography (Wilson 1992). The crystal structure solution allowed the location of twelve independent Ag and Sb sites, whereas following difference-Fourier syntheses led to the finding of nine S positions. The isotropic refinement converged to \(R_1 = 0.14\), thus suggesting the correctness of the structural model. Owing to the similar scattering factors of Ag
(Z = 47) and Sb (Z = 51), these two atoms were located on the basis of their coordination environment and bond-valence sums (BVS). All sites were found to be fully occupied. After several cycles of anisotropic refinement for all atoms, the final statistical factor $R_1$ converged to 0.0626 for 2682 unique reflections with $F_o > 4\sigma(F_o)$ and 191 refined parameters.

Given the relatively large atomic displacement parameters (ADP) of some of the Ag atoms (as typical of fast ion conducting phases - the average ADP values of the nine Ag positions was 0.046 Å$^2$, to be compared with 0.019 Å$^2$ for the three Sb sites), an attempt to refine the crystal structure using higher order tensor elements in the expression of the structure factor (the “non harmonic approach” – Johnson and Levy 1974; Zucker and Schulz 1982) was tried. As documented by Bindi and Evain (2007), this alternative approach, in particular the Gram-Charlier formalism which is recommended by the IUCr Commission on Crystallographic Nomenclature (Trueblood et al. 1996), provides an easier convergence on the refinement, due to much lower correlations between the refined parameters. The new refinement was carried out using the software JANA2006 (Petříček et al. 2006). However, the occurrence of negative regions in the probability density function maps indicated the inadequacy of the results. Consequently, the Gaussian approximation was preferred.

Details of the intensity data collection and crystal structure refinement are given in Table 4. Selected bond distances are listed in Table 5. Bond-valence sums, calculated using the bond parameters of Brese and O'Keeffe (1991), are shown in Table 6. The Crystallographic Information File (CIF), including atomic coordinates and reflection data, is available as Supplementary Material.

**CRYSTAL STRUCTURE ANALYSIS**

**Crystal structure description**

The crystal structure of pyradoketosite (Fig. 3) shows the presence of twelve cation sites and nine anion positions. Among the cation sites, nine are occupied by Ag$^+$ and three by Sb$^{3+}$. Two different but complementary approaches can be used for the description of the crystal structure, i.e.,
according to the distribution of strong (= short) and weak (= long) bonds, or cutting the structure according to \{101\} layers having different chemical compositions.

Considering the shortest (= strongest) bonds, isolated SbS$_3$ trigonal pyramids can be observed organized according to \{101\} layers, with the pyramidal vertices alternately oriented towards [10-1] and [101] (Fig. 3). Antimony atoms show average \(\langle Sb–S \rangle\) distances ranging between 2.429 Å and 2.465 Å (Table 5), comparable with 2.444 Å and 2.460 Å for pyrargyrite and pyrostilpnite (Laufek et al. 2010; Biagioni et al. 2020c), respectively. The BVS of Sb atoms (Table 6) ranges between 2.88 and 3.19 valence units (v.u.).

In Figure 3, \{-102\} layers sub-perpendicular to SbS$_3$ layers can be observed. One slab is partly represented in Figure 4. The Ag atom hosted at the Ag(2) site forms two strong bonds with two symmetry-related S(4) atoms (at 2.46 and 2.47 Å) and a longer bond at 2.72 Å with S(7). These S atoms belong to three different Sb(2)S$_3$ groups. In this way, an \([Ag(2)Sb(2)S$_3$]^{2-}\) ribbon can be distinguished. In this ribbon, Ag(2) atoms form with S(4) atoms a zig-zag chain running along \(b\), decorated on both sides by Sb(2)S$_3$ trigonal pyramids. An additional longer bond at 2.86 Å completes the coordination environment of Ag(2). A similar configuration involves Ag(9) atoms, forming with S(2) atoms a zig-zag chain decorated by Sb(1)S$_3$ trigonal pyramids. It gives the ribbon \([Ag(9)Sb(1)S$_3$]^{2-}\).

The Sb(3)S$_3$ group shares its three S atoms with Ag atoms hosted at Ag(3). Along \(b\), Sb(3)S$_3$ groups and Ag(3) alternate, forming a rod of composition \([Ag(3)Sb(3)S$_3$]^{2-}\). This rod is connected to the adjacent \([Ag(2)Sb(2)S$_3$]^{2-}\) ribbon through the Ag(1) site, whereas it is bonded to the \([Ag(9)Sb(1)S$_3$]^{2-}\) ribbon through the Ag(4) site (Fig. 4). Both Ag(1) and Ag(4) sites have a three-fold coordination. However, the coordination of Ag(1) is increased to four owing to the occurrence of an additional longer bond at 2.96 Å. The bonding of the (Ag/Sb) rod and the two (Ag/Sb) ribbons gives rise to the \{-102\} layer with chemical composition \([Ag_5Sb_3S_9]^{4-}\) (Fig. 3). Such layers are bonded along [-101] owing to the occurrence of three-fold coordinated Ag atoms hosted at the...
Ag(5), Ag(6), Ag(7), and Ag(8) sites (Fig. 3). Considering all Ag atoms, average \( \langle Ag-S \rangle \) distances range between 2.525 Å for the three-fold coordinated Ag(9) site and 2.629 Å for the four-fold coordinated Ag(2) position (Table 5). The BVS at the Ag sites varies between 0.94 and 1.22 v.u. (Table 6). The shortest Ag–Ag distance is 2.970(2) Å for the pair Ag(3)–Ag(7). The Ag–Sb distances are usually longer than 3.30 Å; however, a very short Ag–Sb distance occurs for the pair Ag(3)–Sb(1), i.e., 2.966(2) Å. This short distance may be indicative of an average position of the Ag(3) atom which could not be resolved in two sub-positions.

An alternative description of the crystal structure of pyradoketosite considers the occurrence of chemically different \{101\} layers. Figure 5 shows the organization of the crystal structure according to this \{101\} layered arrangement. This description is particularly useful in pointing out the relationship between pyradoketosite and the members of the wittichenite-skinnerite group (see below).

The crystal-chemical formula of pyradoketosite, derived from the crystal structure study, is \( Ag_3SbS_3 (Z = 12) \).

**Comparison with other \( Ag_3SbCh_3 \) (\( Ch = S, Se \)) compounds**

The compound \( Ag_3SbS_3 \) is known in nature since the 19th Century as pyrargyrite (trigonal, \( R3c \)) and pyrostilpnite (monoclinic, \( P2_1/c \)). The replacement of Sb by As gives rise to proustite, showing isotypic relations with pyrargyrite, and xanthococonite (monoclinic, \( C2/c \)) (e.g., Bindi and Biagioni 2018 and references therein). Eckerite, ideally CuAg\(_2\)AsS\(_3\), is a Cu-bearing isotype of xanthococonite (Bindi et al. 2015). Table 7 compares pyradoketosite with these natural phases and with the three synthetic Ag-compounds having a similar stoichiometry.

The crystal structure of pyradoketosite is different from those of the other two naturally-occurring polymorphs, pyrargyrite (and its Se synthetic isotype) and pyrostilpnite, as well as from those of the synthetic orthorhombic \( Ag_3XSe_3 \) phases, where \( X = As, Sb \). The crystal structure of
pyrargyrite is characterized by columns of SbS$_3$ pyramids running along $c$, with the orientation of
their vertices preserved along the polar three-fold $c$ axis. Silver atoms have a linear two-fold
coordination and give rise to spirals running along [001] (Engel and Nowacki 1966; Laufek et al.
2010). In pyrostilpnite, \{010\} (Ag/Sb) layers, corresponding to (210)$_{PbS}$ slabs, run along $c$ and are
connected through longer Ag–S bonds (Kutoglu 1968; Biagioni et al. 2020c). Antimony atoms
decorate these layers, and the lone-electron-pairs are directed in the space between successive layers
along $b$. The coordination number of Ag atoms in pyrostilpnite varies from two to four. As
described above, the crystal structure of pyradoketesite can be described as formed by \{-102\} layers
connected by additional Ag atoms. Silver coordination is mainly triangular, with only one atom at
the Ag(2) site having two-fold coordination.

A different packing density is also suggested by the calculation of the cell volumes for one
Ag$_3$SbS$_3$ unit. Pyradoketesite is slightly less-densely packed ($V = 154.8$ Å$^3$) with respect to
pyrargyrite ($V = 153.6$ Å$^3$) and pyrostilpnite ($V = 152.1$ Å$^3$). This is reflected by the calculated
densities, increasing from pyradoketesite (5.81 g/cm$^3$) to pyrostilpnite (5.97 g/cm$^3$), passing through
pyrargyrite (5.86 g/cm$^3$).

**Relationship with the wittichenite-skinnerite homeotypic pair**

On the basis of the Sb layering described in Figure 5, a supercell has been selected. This
supercell can be derived from the $P2_1/n$ cell through the transformation matrix $R = [1 \ 0 \ -1 \ | \ 0 \ 1 \ 0 \ | \ 1 \ 0 \ 1]$ which gives the unit-cell parameters $a = 24.831(2)$, $b = 6.9350(6)$, $c = 22.944(2)$ Å, $\beta =
109.835(8)^\circ$, $V = 3716.6(6)$ Å$^3$. It shows the alternation with the Sb-rich layer, AgSb$_3$S$_3$, of two
distinct Ag$_8$S$_6$ layers (A and B). Considering the distribution of short (= strong) Ag–S distances
(Ag–S < 2.75 Å), each Ag$_8$S$_6$ layer can be considered as the sum of 2Ag$_3$S$_2$ + Ag$_2$S$_2$. Such an
organization directly relates to the crystal structure of the wittichenite-skinnerite homeotypic pair
(Moëlo et al. 2008). The crystal structure of wittichenite was independently solved by Matzat
(1972) and Kocman and Nuffield (1973) (Fig. 6a), whereas that of skinnerite was solved by Pfitzner (1994) and Makovicky and Balić-Žunić (1995) (Fig. 6b). One BiS or SbS layer alternates with one Cu$_3$S$_2$ layer. BiS and SbS layers are equivalent, while Cu distribution differs between the two structures.

Two synthetic Li-sulfides, Li$_3$SbS$_3$ and Li$_3$AsS$_3$, relate to this group (Huber et al. 2012) and are isotypic (Fig. 6c). The coordination of Li atoms is tetrahedral (two positions) or square pyramidal (one position), whereas Cu coordination in wittichenite and skinnerite is exclusively triangular.

Table 8 compares the unit-cell parameters of all these compounds. For the reduced unit cell (basis: 4 formula units), the stacking parameter is close to 10 Å, and the two in-plane parameters are close to 8 and 6.8 Å. Unit-cell volumes are in the range 530-545 Å$^3$. For “average pyradoketosite” (i.e., the reduced cell containing 4 formula units), Ag-for-Cu substitution increases all parameters relative to skinnerite: $b + 12\%$, $a + 6\%$, $c + 4.5\%$, $V + 17\%$.

Pyradoketosite appears as a derivative of wittichenite with a (2 × 3) superstructure (Table 8), with developed crystal chemical formula (Ag$_3$S$_2$)$_2$(Ag$_3$S$_2$)(Sb$_3$AgS$_3$) = Ag$_9$Sb$_3$S$_9$. In the other members of this group, while the (Bi/Sb/As)S layers are topologically identical, the adjustment of the intercalated (Cu/Li)$_3$S$_2$ layer proceeds in two different ways. In wittichenite and skinnerite, Cu coordination is triangular (ideal Cu–S distance: 2.27 Å), whereas in Li$_3$SbS$_3$, there are two LiS$_4$ tetrahedra and one LiS$_5$ square pyramid (ideal Li–S distances: 2.45 and 2.55 Å, respectively). In pyradoketosite, with Ag coordination mainly triangular (ideal Ag–S distance: 2.56 Å), due to the increase of the size of Ag$^+$ relatively to Cu$^+$ or Li$^+$, the steric adjustment is realized through the transfer of one Ag atom among nine from the Ag$_3$S$_2$ layer to the SbS layer, reducing the expansion of the former layer and expanding the latter. Pyradoketosite is a plesiotypic derivative of wittichenite, according to the definition of Makovicky (1997).
The uneven intra-layer superstructure (× 3) imposes a monoclinic stacking. The differentiation of two distinct Ag₈S₆ layers (A and B) results from Ag(3) pairing across the A layer (double black arrow in Figure 5), giving an Ag–Ag distance of 5.39 Å and, inversely, a longer distance across the B layer (8.17 Å).

**GENESIS OF PYRADOKETOSITE**

The occurrence of pyradoketosite reveals that unexpected complex crystal structures can occur in the Ag–Sb–S system. Details of this chemical system have been studied since the 1930s (see Keighin and Honea 1969 and references therein). Several researchers tried to describe the relationships between the products of experimental runs and the observed mineral assemblages, to use some of them as geothermometers. Pyrargyrite, the most common polymorph of Ag₃SbS₃, has been easily obtained in several synthesis experiments (e.g., Barstad 1959; Keighin and Honea 1969; Hoda and Chang 1975). On the contrary, pyrostilpnite was reported by Weil and Hocart (1953) in a synthesis carried out under glycerol. Their results, however, could not be reproduced by Keighin and Honea (1969). Chang (1963) observed that pyrostilpnite can invert into pyrargyrite under heating at 197°C for 300 h; on the contrary, pyrargyrite, heated at 150°C for 350 h, does not invert to pyrostilpnite. Keighin and Honea (1969) proposed an inversion temperature of 192 ± 5°C for the pyrostilpnite-pyrargyrite transition. It is worth noting that these authors underlined the experimental difficulties in attaining equilibrium assemblages, related to the sluggishness of the reaction kinetics below 300°C, requiring long-term runs (longer than one year), with the possible formation of non-equilibrium assemblages.

In this respect, the occurrence of pyradoketosite is an interesting conundrum. Such a phase, to the best of our knowledge, has not been obtained in any synthetic run (e.g., Goodell 1975 and references therein). Moreover, the crystal-chemical study excludes the possible role of minor constituents in the crystallization of pyradoketosite. The close examination of the spatial relations...
between the three Ag₃SbS₃ polymorphs shown in Figure 1 can help in putting forward some hypotheses. Pyradoketosite is apparently overgrown by probable pyrostilpnite, whereas the latter is overgrown by the equant crystal of pyrargyrite. A first hypothesis could be that this association may represent the result of the co-precipitation of the three Ag₃SbS₃ polymorphs. On the contrary, taking into account the spatial relations among the three phases and considering that pyrostilpnite should invert to pyrargyrite above 192 ± 5°C, one could suppose that the sequence pyradoketosite → pyrostilpnite → pyrargyrite could be the result of an ephemeral prograde variation of $T$, not able to invert the low-$T$ polymorphs into pyrargyrite. However, the role of other physical-chemical parameters (e.g., $p$H, Eh) or kinetic factors is currently unknown. Biagioni et al. (2020a) reported the results of microthermometric investigations performed on fluid inclusions hosted in quartz crystals from the same kind of baryte + dolomite ± quartz veins (occurrence of type C following Biagioni et al. 2020a) where pyradoketosite was found. In these veins, two generations of fluid inclusions occur. The first one has a modal homogenization temperature of 275°C (range 265-289°C), whereas a second generation of fluid inclusion homogenizes at 235°C (range 222-246°C). Pyradoketosite was observed in dissolution cavities, along with valentinite, and seems to be a late-stage mineral. Consequently, its crystallization may be due to a late-stage hydrothermal event, possibly corresponding to the second generation of fluid inclusions hosted in quartz crystals or to a later-stage (and likely cooler) event not recorded in the samples studied by Biagioni et al. (2020a).

**IMPLICATIONS**

One of the main questions for Mineralogy of the 21st Century is about the role played by the description of new mineral species. More and more Earth scientists consider this endeavor as a trivial, not important job, mainly because of the usual uniqueness of the discovered new minerals and their volumetric insignificance, apparently not playing any fundamental role in the Earth dynamics. For instance, the finding of pyradoketosite is limited to just a few crystals, with a total
volume less than 1 mm$^3$, thus fitting the definition of rarity given by Hazen and Ausubel (2016), and its crystallization is likely constrained by a narrow $P$-$T$-$X$ space. However, samples of pyrostilpnite exhibiting an acicular morphology could have been misidentified and actually be pyradoketosite.

In our opinion, the description of a new, rare mineral species as, for instance, pyradoketosite cannot be considered as a mere crystal chemical exercise. Its finding improves our knowledge of the Ag–Sb–S system, where the ternary compounds AgSbS$_2$ and Ag$_3$SbS$_3$ are actively used for their thermoelectric properties as well as for their potential optical applications. Yet, pyrargyrite has long been considered as a promising functional material for several opto-electronic and data storage applications (e.g., Adler 1980) and its physical and thermodynamic properties have been deeply investigated (e.g., Lange et al. 1993; Schönau and Redfern 2002; Aspiala et al. 2016). Furthermore, pyradoketosite highlights the limits of laboratory experiments trying to synthesize complex sulfides to reproduce ore mineral assemblages. As previously discussed by Keighin and Honea (1969), the slowness of reaction rates below 300°C requires very long-term experiments for achieving equilibrium assemblages, thus representing an important limit to the study of low-$T$ ore associations. Consequently, the accurate mineralogical investigation of natural occurrences, where the “synthesis experiments” performed by nature did not suffer from the time constraints typical of human activities, remains a precious and irreplaceable way to discover novel crystal structures and to find complex, unpredictable phases, whose genesis can be related to the wide range of possible $P$-$T$-$X$ conditions occurring on Earth (e.g., Bindi et al. 2020).

Pyradoketosite, the new Ag$_3$SbS$_3$ polymorph, is thus a good example of the usefulness of looking for and studying new mineral species.

Finally, even if it is undeniably true that to understand and get a first plausible picture of most of the geological phenomena occurring on our planet a dozen minerals might be considered sufficient, we think that rare phases can help to provide a more exhaustive scenario of the Earth
dynamics. In other words, with the well-known rock-forming minerals you get an unquestionably
correct picture, but still incomplete. Rare phases, and the stories they tell us, can shed light on
unusual geological processes and provide the hints to refine and progressively improve the scenario
itself.

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Terrestrial and Extraterrestrial ORE Minerals”, prot. 2017AK8C32.

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TABLE CAPTIONS

Table 1 – Reflectance data (%) for pyradoketosite in air.

Table 2 – Electron-microprobe data (mean of 5 spot analyses, in wt%) of pyradoketosite and atoms per formula unit (apfu) on the basis of 4 (Ag+Sb) apfu.

Table 3 – Observed and calculated X-ray powder diffraction data for pyradoketosite. Intensity and $d_{hkl}$ were calculated using the software PowderCell2.3 (Kraus and Nolze 1996) on the basis of the refined structural model. Only reflections with $I_{\text{calc}} > 10$ are listed, if not observed. The five strongest calculated reflections are given in bold. Observed intensities were visually estimated (s = strong; mw = medium-weak; w = weak).

Table 4 – Crystal data and summary of parameters describing data collection and refinement for pyradoketosite.

Table 5 – Selected bond distances (in Å) for pyradoketosite.

Table 6 – Bond valence sums (in valence units, v.u.) for pyradoketosite.

Table 7 – Natural and synthetic compounds chemically related to pyradoketosite.

Table 8 – Comparison of unit-cell parameters of members of the wittichenite-skinnerite group with parameters of the supercell of pyradoketosite (see dotted lines in Figure 5).

FIGURE CAPTIONS

Fig. 1 – Pyradoketosite, striated acicular crystals, orange in color (a). Scanning electron microscope image shows the association with equant pyrargyrite and probable tabular pyrostilpnite (b). Sant’Olga tunnel, Monte Arsiccio mine, Apuan Alps, Tuscany, Italy. Holotype material.

Fig. 2 – Reflectance spectrum of pyradoketosite (square), compared with those of pyrargyrite (triangles) and pyrostilpnite (circles). $R_1$ and $R_2$ are shown as dotted and dashed lines, respectively. Data for pyrargyrite and pyrostilpnite are after Criddle and Stanley (1986).

Fig. 3 – Crystal structure of pyradoketosite projected down b. The organization of SbS$_3$ groups in two {101} layers having different polarity is shown (arrows indicate the orientation of SbS$_3$ pyramids). Numbers indicate the Ag (violet) and Sb (green) sites. Dashed red lines indicate the unit cell, whereas blue dashed lines highlight {−102} layers.

Fig. 4 – Organization of {−102} layers [without marginal Ag(5) and Ag(8) atoms].

Fig. 5 – The {101} layered organization of pyradoketosite as seen down b. Grey dotted lines show two unit cells, whereas dotted red lines represent the supercell discussed in the text. Numbers “2”
and “3” indicate the $\text{Ag}_2\text{S}_2$ and $\text{Ag}_3\text{S}_2$ groups. Double black arrows show the Ag(3) pairing across the A layers.

**Fig. 6** – Crystal structures of wittichenite (a), skinnerite (b), and $\text{Li}_3\text{Sb}_3\text{S}_3$ (c) as seen down $\mathbf{b}$.
Table 1 – Reflectance data (%) for pyradoketosite in air.

<table>
<thead>
<tr>
<th>λ/nm</th>
<th>$R_1$</th>
<th>$R_2$</th>
<th>λ/nm</th>
<th>$R_1$</th>
<th>$R_2$</th>
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<td>560</td>
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<td>30.3</td>
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<tr>
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<td>35.6</td>
<td>580</td>
<td>29.2</td>
<td>29.8</td>
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<tr>
<td>440</td>
<td>34.0</td>
<td>34.3</td>
<td>589</td>
<td>29.0</td>
<td>29.6</td>
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<td>460</td>
<td>33.0</td>
<td>33.3</td>
<td>600</td>
<td>28.7</td>
<td>29.3</td>
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<td>470</td>
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<td>32.9</td>
<td>620</td>
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<td>480</td>
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<td>32.4</td>
<td>640</td>
<td>27.7</td>
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<td>500</td>
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<td>31.9</td>
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<td>28.4</td>
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<tr>
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<td>660</td>
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<td>28.2</td>
</tr>
<tr>
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<td>680</td>
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<tr>
<td>546</td>
<td>30.2</td>
<td>30.7</td>
<td>700</td>
<td>26.7</td>
<td>27.9</td>
</tr>
</tbody>
</table>

Note: data for the four COM wavelengths are given in bold.
Table 2 – Electron-microprobe data (mean of 5 spot analyses, in wt%) of pyradoketosite and atoms per formula unit (apfu) on the basis of 4 (Ag+Sb) apfu.

<table>
<thead>
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<th>Element</th>
<th>wt%</th>
<th>Range</th>
<th>e.s.d.</th>
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<tr>
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<td>58.90 – 60.21</td>
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<tr>
<td>Sb</td>
<td>22.63</td>
<td>22.41 – 22.87</td>
<td>0.19</td>
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<tr>
<td>S</td>
<td>17.78</td>
<td>17.55 – 17.92</td>
<td>0.14</td>
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<tr>
<td>Total</td>
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<td>99.31 – 100.66</td>
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<table>
<thead>
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<th>apfu (ΣMe = 4)</th>
<th>Range</th>
<th>e.s.d.</th>
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<tr>
<td>Ag</td>
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<td>2.976 – 3.007</td>
</tr>
<tr>
<td>Sb</td>
<td>1.004</td>
<td>0.993 – 1.024</td>
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<tr>
<td>S</td>
<td>2.996</td>
<td>2.983 – 3.015</td>
</tr>
<tr>
<td>Ev (%)</td>
<td>0.3</td>
<td>-0.7 – 1.4</td>
</tr>
</tbody>
</table>

Note: $Ev(\%) = \left[ Σ(val+) - Σ(val-) \right] \times 100 / Σ(val-)$. 

539
Table 3 – Observed and calculated X-ray powder diffraction data for pyridoketosite. Intensity and \(d_{hkl}\) were calculated using the software *PowderCell*2.3 (Kraus and Nolze 1996) on the basis of the refined structural model. Only reflections with \(I_{\text{calc}} > 10\) are listed, if not observed. The five strongest calculated reflections are given in bold. Observed intensities were visually estimated (s = strong; mw = medium-weak; w = weak).

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<th>(I_{\text{obs}})</th>
<th>(d_{\text{obs}})</th>
<th>(I_{\text{calc}})</th>
<th>(d_{\text{calc}})</th>
<th>(h k l)</th>
<th>(I_{\text{obs}})</th>
<th>(d_{\text{obs}})</th>
<th>(I_{\text{calc}})</th>
<th>(d_{\text{calc}})</th>
<th>(h k l)</th>
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Table 4 – Crystal data and summary of parameters describing data collection and refinement for pyradoketosite.

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<td>Monoclinic, P2₁/n</td>
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<td>a (Å)</td>
<td>13.7510(15)</td>
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<td>b (Å)</td>
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<td>c (Å)</td>
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Data collection and refinement

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<td>Maximum and minimum residual peak (e Å⁻³)</td>
<td>3.09 [at 1.00 Å from Ag(8)] and -2.93 [at 0.86 Å from Ag(8)]</td>
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Table 5 – Selected bond distances (in Å) for pyradoketosite.

<table>
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<th></th>
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<th>S(8)</th>
<th>S(3)</th>
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<tr>
<td>Ag(2)</td>
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<td>–</td>
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<td>S(4)</td>
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Average: 2.628 Å

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Average: 2.465 Å
Table 6 – Bond valence sums (in valence units, v.u.) for pyradoketosite.

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Table 7 – Natural and synthetic compounds chemically related to pyradoketosite.

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<th>c (Å)</th>
<th>α (°)</th>
<th>β (°)</th>
<th>γ (°)</th>
<th>V (Å³)</th>
<th>S.g.</th>
<th>Z</th>
<th>Ref.</th>
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<td>10.84</td>
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Table 8 – Comparison of unit-cell parameters of members of the wittichenite-skinnerite group with parameters of the supercell of pyradoketosite represented in Figure 5.

<table>
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<th>A' (Å)</th>
<th>A'' (Å)</th>
<th>S (Å)</th>
<th>Oblique angle (°)</th>
<th>V (Å³)</th>
<th>Ref.</th>
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Fig. 3
Fig. 4